



Calorimetry

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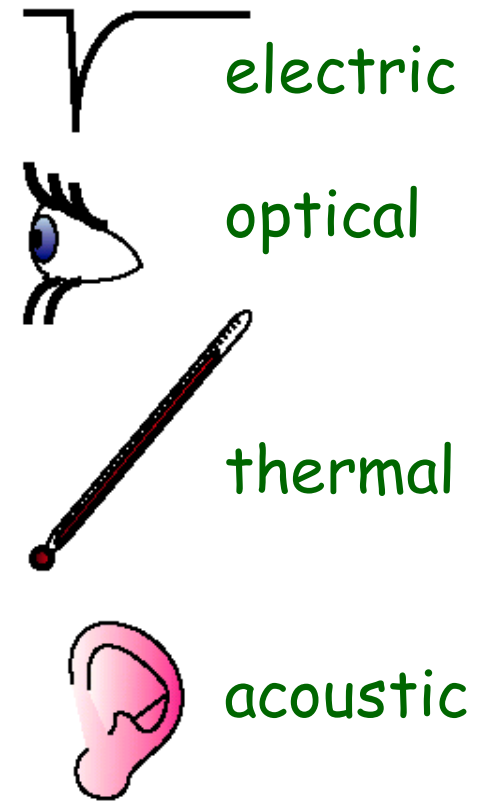
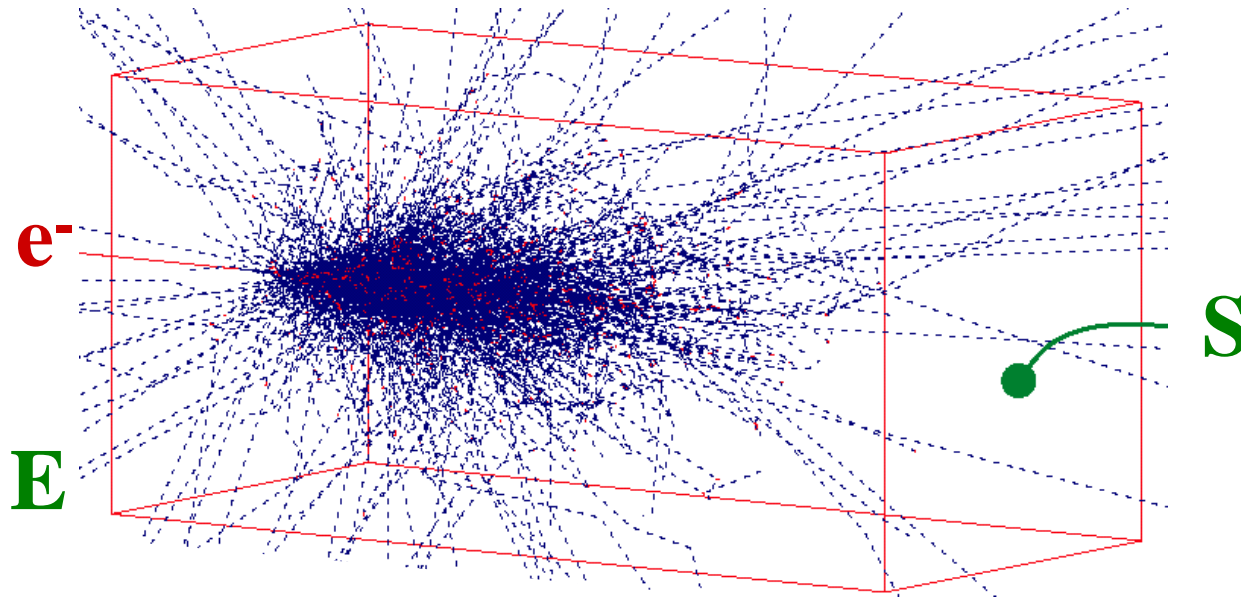
[Outline]

The talk is an introduction to calorimetry with focus on the CMS electromagnetic and hadronic calorimeters

- Particle interaction with matter
- Electromagnetic and hadronic showers
- Detection mechanisms
- Homogeneous and sampling calorimeters
- Energy resolution
- Compensation & Energy Flow
- The CMS calorimeters
- Few examples about performance of CMS calorimeters

Suggested reading: Calorimetry
by Richard Wigmans
Many plots taken from his talks.

Calorimeters: a simple concept



Convert energy E of incident particle
to detector response S : $S \propto E$

The temperature effect of a 100 GeV particle in
1 litre of water (at 20 °C) is: $\Delta T = 3.8 \cdot 10^{-12} K$

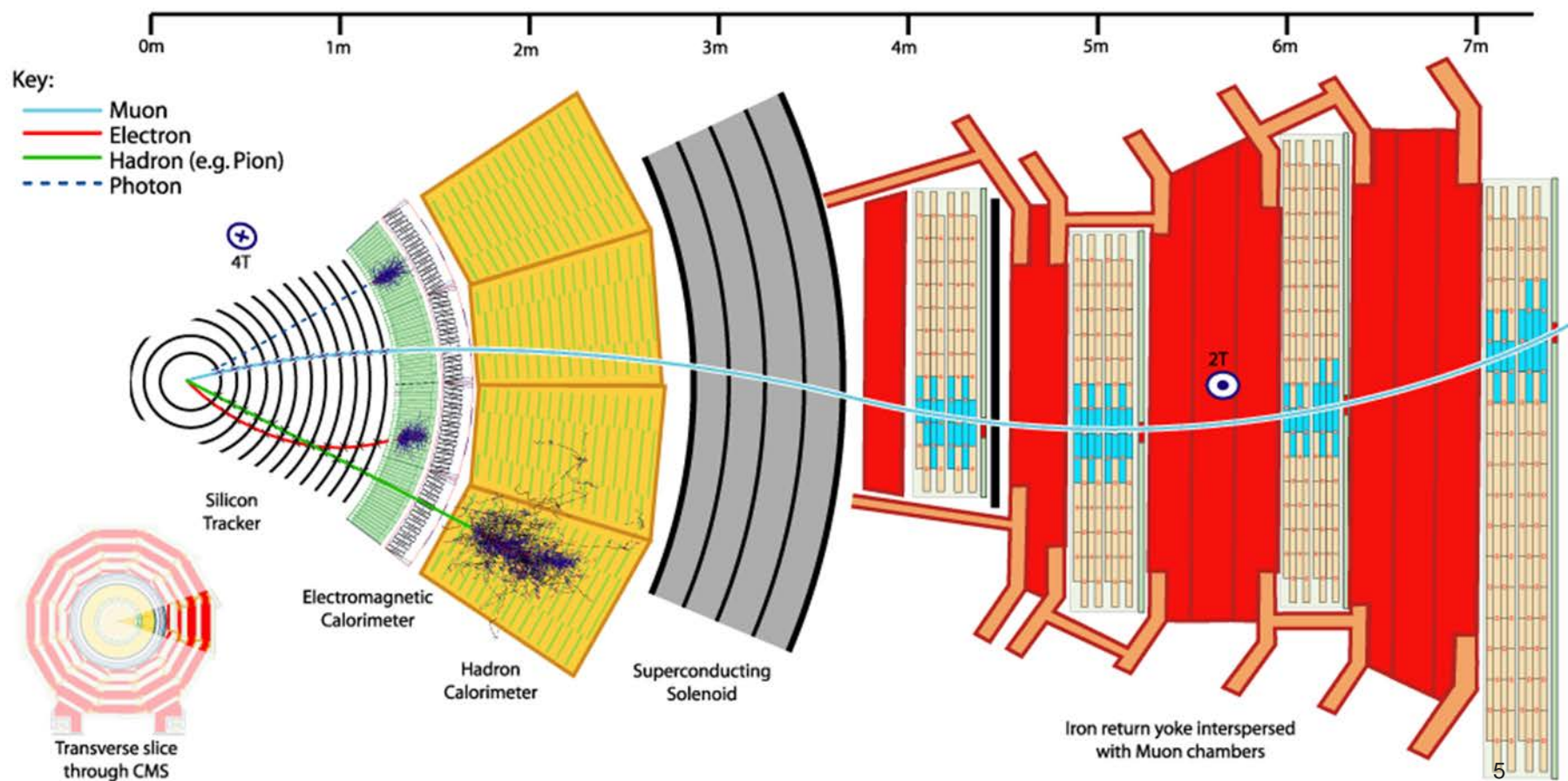
[Calorimeters: some features]

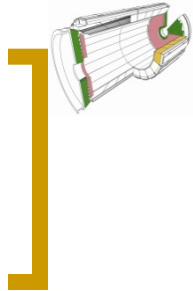
- Detection of both charged and neutral particles
- Particle identification by simple topological algorithms
- Detection based on stochastic processes
precision increases with E
- Dimensions necessary to containment $\propto \ln E$
compactness
- Segmentation
measure of position and direction
- Fast
high rate capability, trigger



Calorimetry is a "destructive" method. Energy and particle get absorbed!

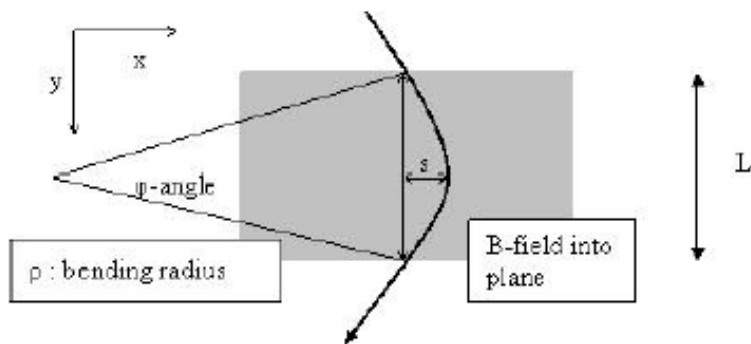
Particles in CMS detector





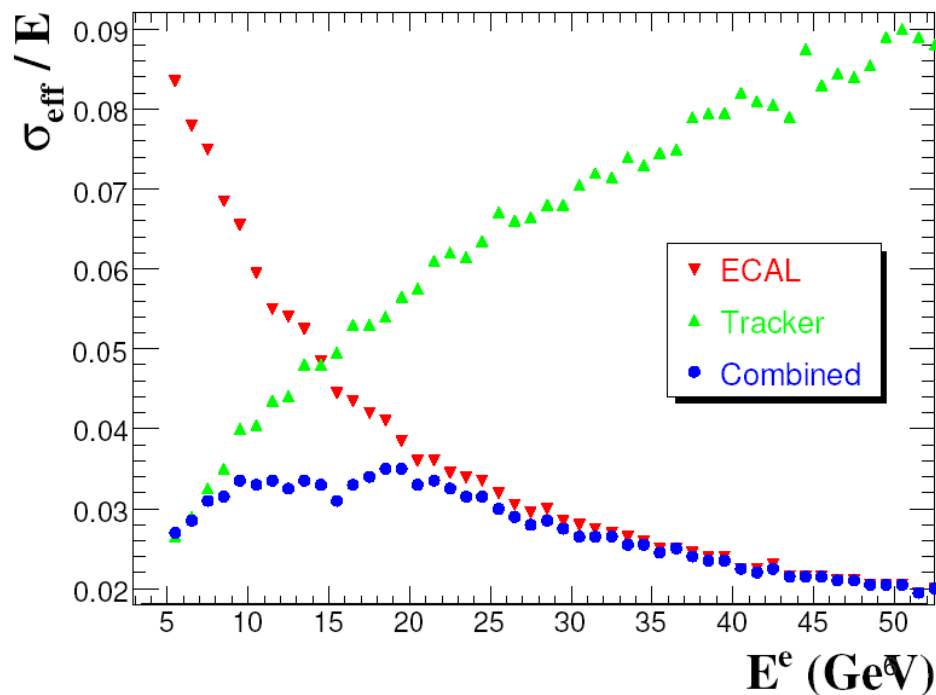
Resolution: calorimeter vs tracker

tracker momentum
measurement with
the sagitta method



$$\frac{\sigma(p_T)}{p_T} = \frac{\sigma(x) p_T}{0.3BL^2} \sqrt{720/(N+4)}$$

In CMS the contribution to the
electron energy measurement
from the tracker is relevant
below ~ 20 GeV.



Energy loss - electrons (1)

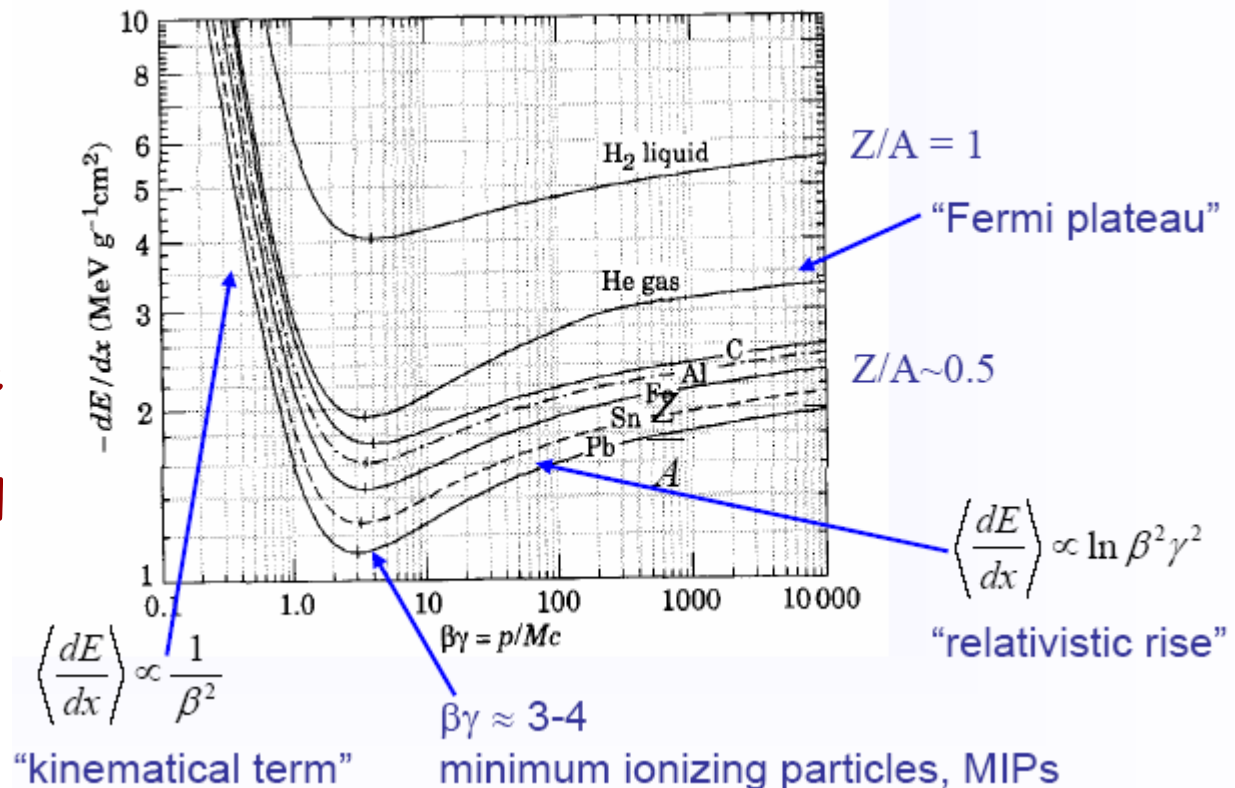
➤ Ionization : mean energy loss given by Bethe-Bloch

$$\left\langle \frac{dE}{dx} \right\rangle = -4\pi N_A r_e^2 m_e c^2 z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2m_e c^2 \gamma^2 \beta^2}{I^2} T^{\max} - \beta^2 - \frac{\delta}{2} \right]$$

$$\sigma \propto Z$$

$$\sigma \propto \ln E/m_e$$

Electrons require some corrections due to their small mass and Pauli principle.



Energy loss - electrons (2)

- bremsstrahlung

➤ energy loss $-\frac{dE}{dx}|_{rad} = \left[4n \frac{Z^2 \alpha^3 (\hbar c)^2}{m_e^2 c^4} \ln \frac{183}{Z^{1/3}} \right] E$

$$-\frac{dE}{dx} \propto \frac{Z^2 E}{m^2}$$

$$\langle \Theta \rangle = \frac{1}{\gamma}$$

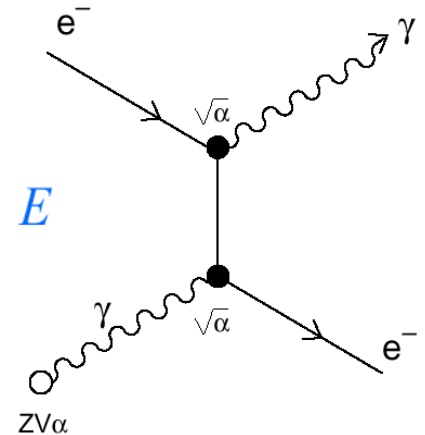
$$X_0 = \left[4n \frac{Z^2 \alpha^3 (\hbar c)^2}{m_e^2 c^4} \ln \frac{183}{Z^{1/3}} \right]^{-1}$$

Radiation length: thickness of material that reduces the mean energy of a beam of high energy electrons by a factor e

$$\frac{dE}{dx} = - \frac{E}{X_0} \quad \text{and} \quad X_0 \approx \frac{180 A}{Z^2} \text{ g.cm}^{-2}$$

in air: 300 m
in plastic scintillator: 40 cm
in iron: 1.76 cm

$\sigma \propto Z(Z+1)$; $\propto \ln E/m_e$ for $E < 1 \text{ GeV}$ independent of energy above



Energy loss - electrons (3)

- Critical energy E_c :

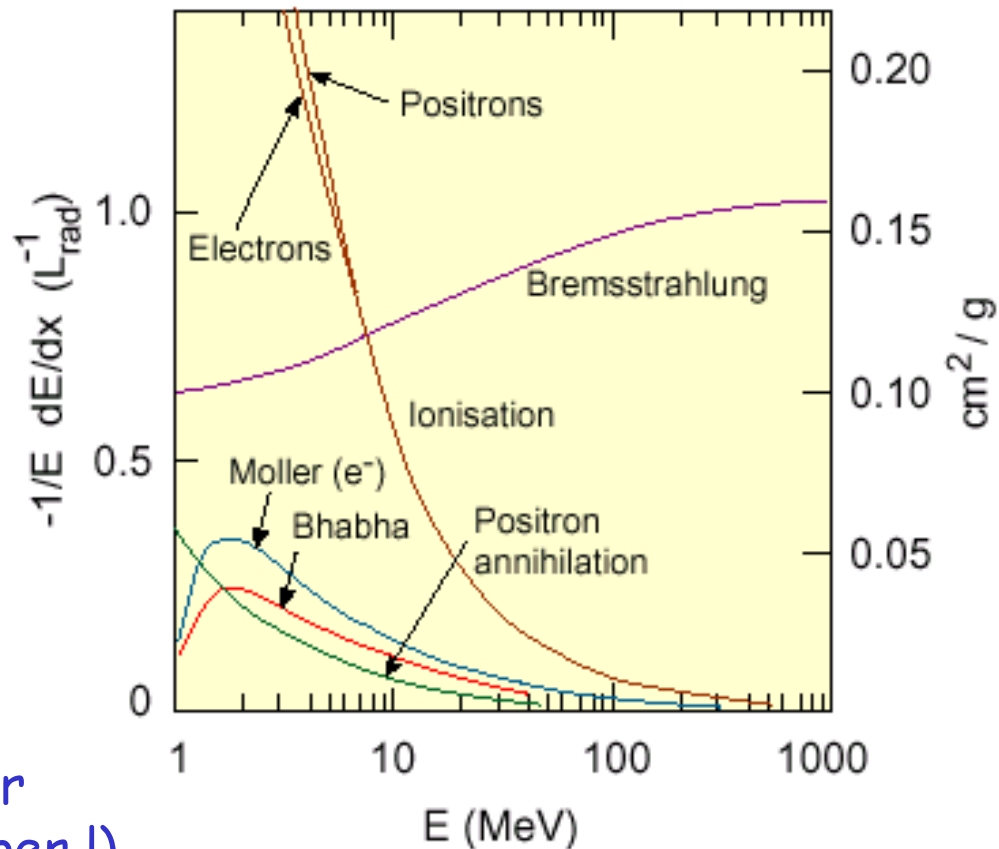
$$\frac{(dE/dx)_{rad}}{(dE/dx)_{ion}} = 1$$

$$E_c \approx \frac{610 \text{ MeV}}{Z + 1.24}$$

(solids, liquids)

Strongly material dependent,
it scales as $1/Z$
(eg. 7 MeV for lead, 20 MeV for
copper; 1 TeV for muons in copper !)

Fractional Energy Loss by Electrons



Energy loss - photons (1)

- photo-electric effect

$$\sigma_{\text{pe}} \approx Z^5 \alpha^4 \left(\frac{m_e c^2}{E_\gamma} \right)^{\frac{7}{2}} \quad \sigma \propto Z^5, E^{-3.5}$$

- compton scattering

$$\sigma_c \approx Z \frac{\ln E_\gamma}{E_\gamma} \quad \sigma \propto Z, E^{-1}$$

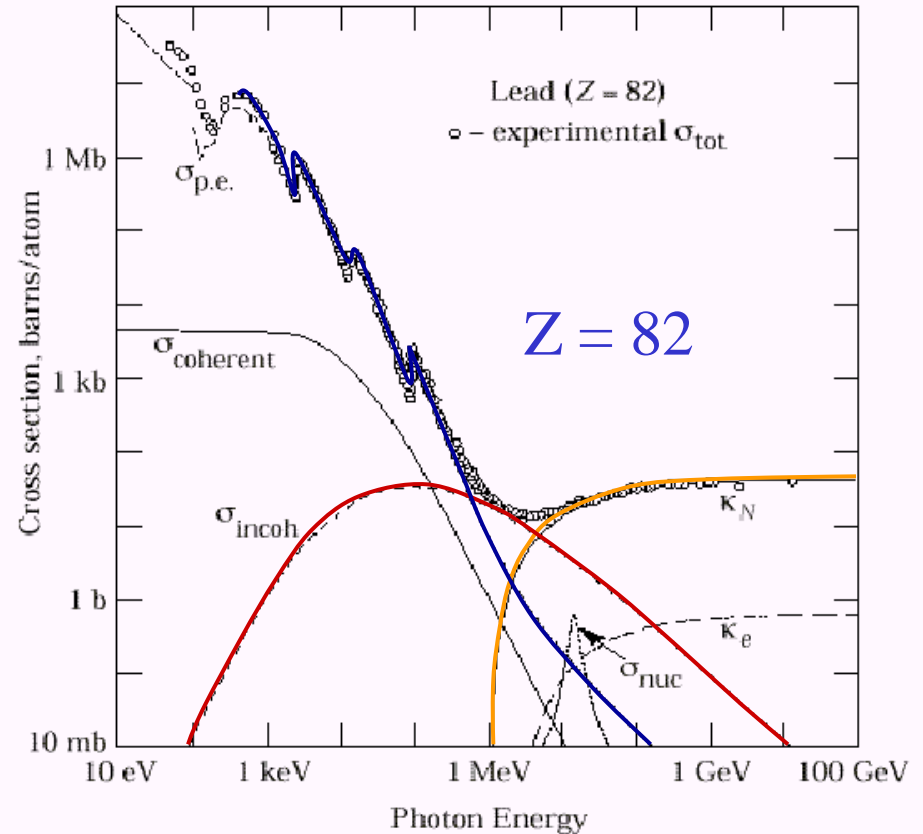
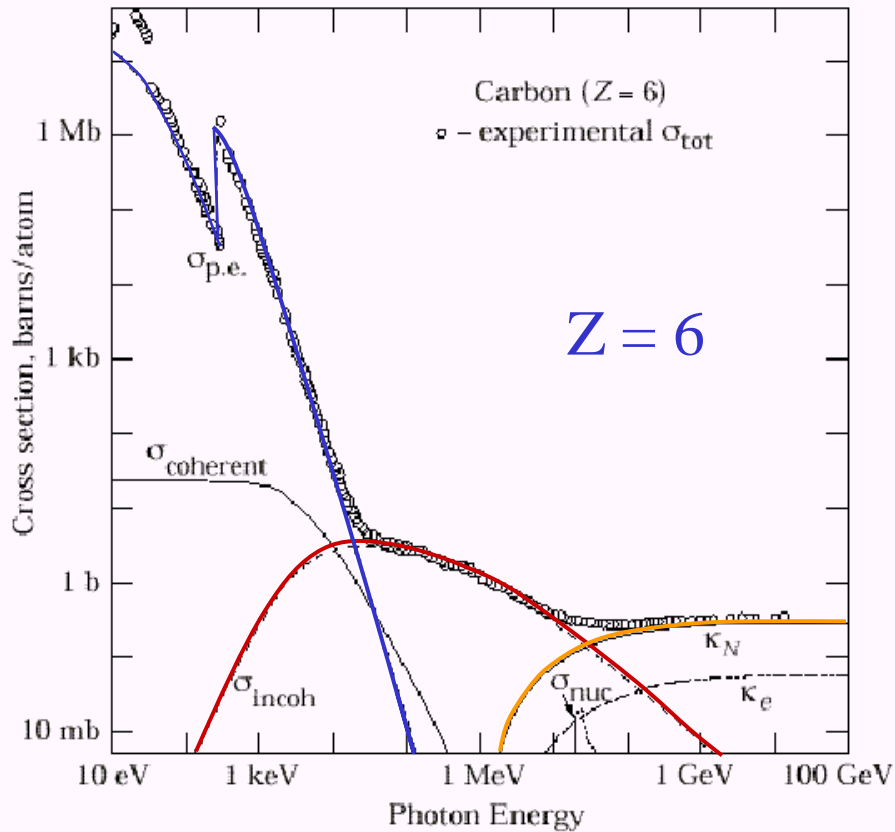
- pair production occurs if $E_\gamma > 2m_e c^2$

$$\sigma_{\text{pair}} \approx \frac{7}{9} \frac{A}{N_A} \frac{1}{X_0}$$

- $\sigma \propto Z(Z+1)$; $\propto \ln E/m_e$ for $E < 1\text{ GeV}$
independent of energy above 1 GeV
- Probability of conversion in $1X_0$ is $e^{-7/9}$
- Mean free path $L_{\text{pair}} = 9/7 X_0$ (γ disappears)

Energy loss - photons (2)

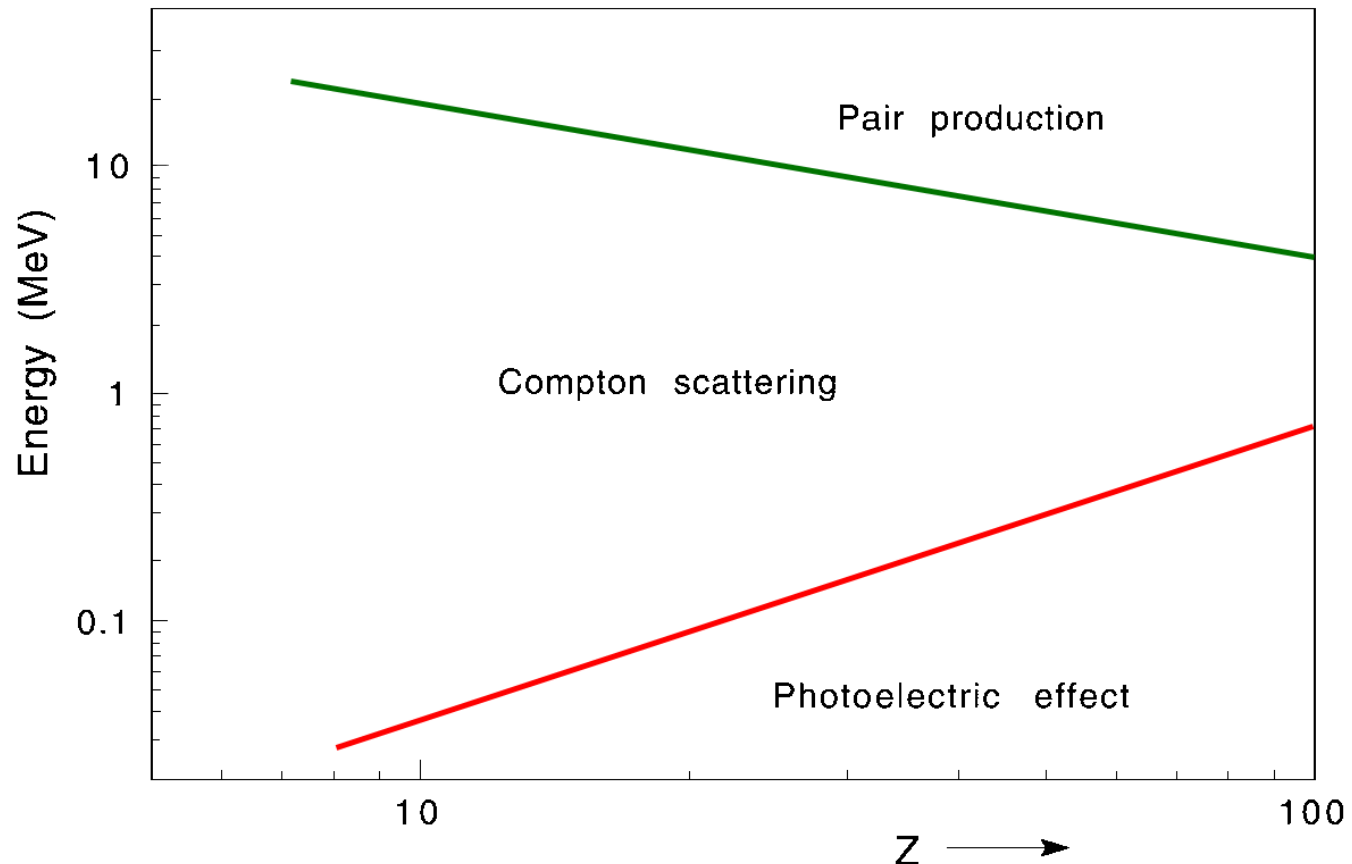
Contributions to Photon Cross Section in Carbon and Lead



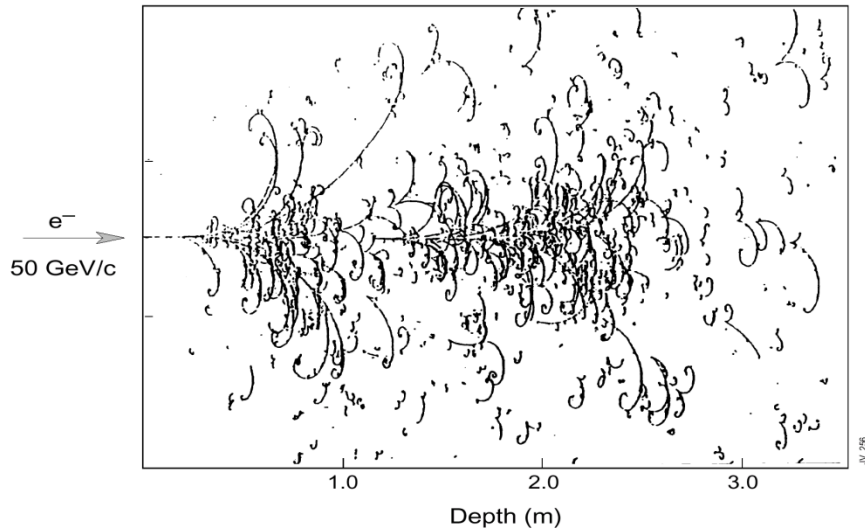
Cross section in right plot: more lead is needed to absorb a photon with 20 MeV energy than a 3 MeV photon !!

Energy loss - photons (3)

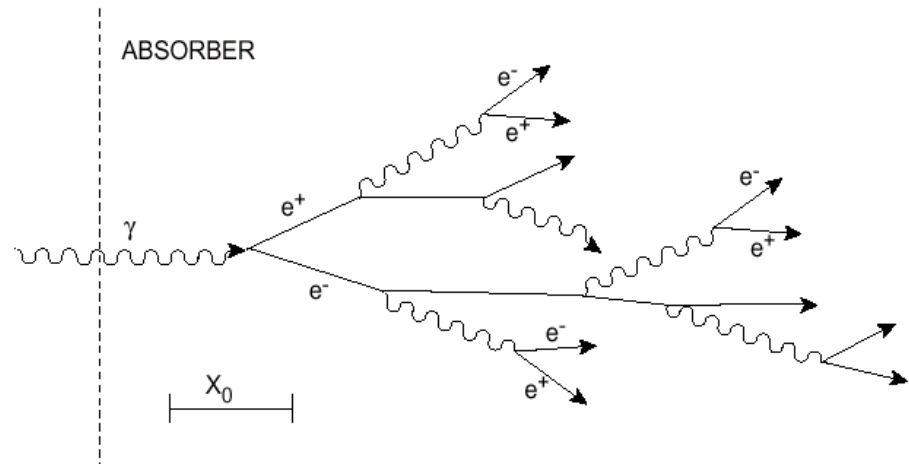
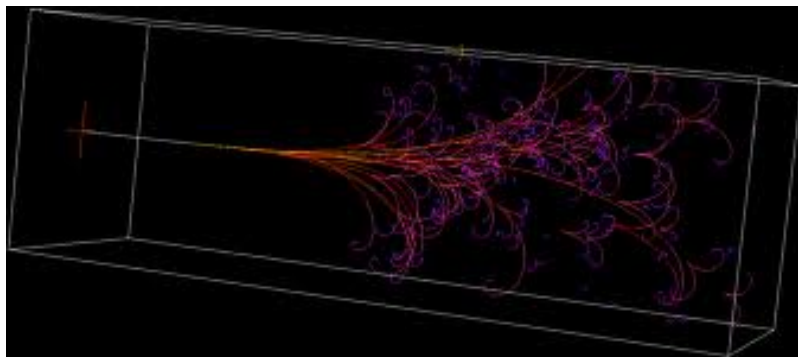
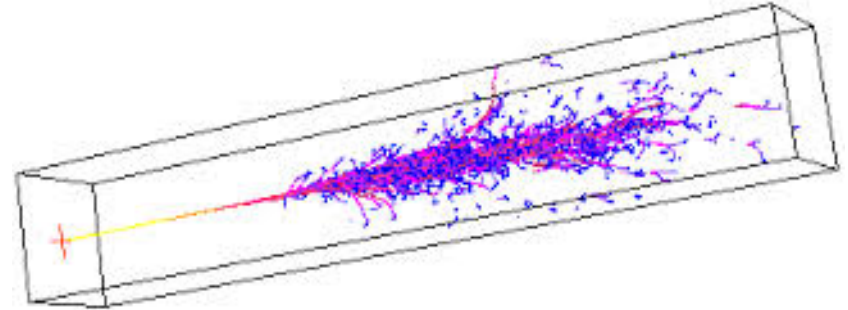
Main contribution to cross section



Electromagnetic Shower



Big European Bubble Chamber filled with $\text{Ne:H}_2 = 70\%:30\%$,
3T Field, $L=3.5$ m, $X_0 \approx 34$ cm, 50 GeV incident electron



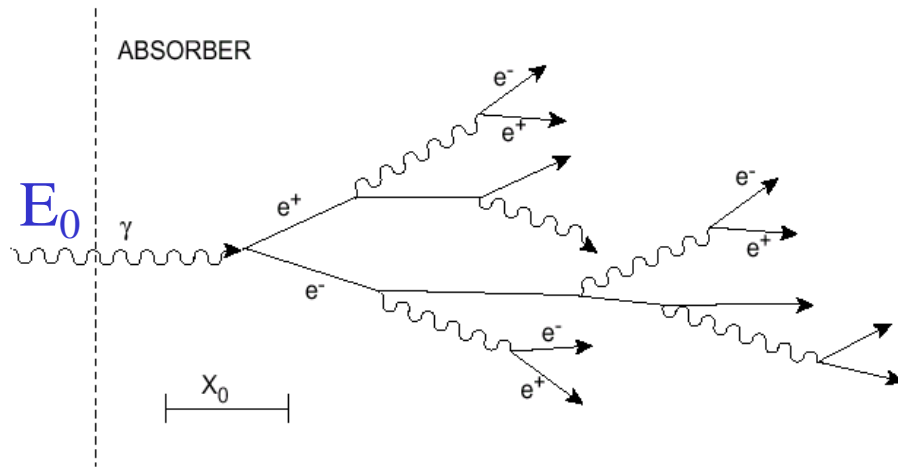
Electromagnetic Shower (2)

Above 1 GeV the dominant processes, bremsstrahlung for e^+ and e^- and pair production for γ , become energy independent

Trough a succession of these energy loss mechanisms an electromagnetic cascade is propagated until the energy of charged secondaries has been degraded to the regime dominated by ionization loss (below E_c)

Below E_c a slow decrease in number of particles occurs as electrons are stopped and photons absorbed

Electromagnetic Shower (3)



- In $1X_0$ an e loses about $2/3$ of its E
a high energy γ has a probability of $7/9$ of pair conversion
- Assume X_0 as a generation length
- In each generation the number of particle increases by a factor 2

@ $\Delta x = X_0$ $\gamma \rightarrow e^+ e^-$ $E = E_0/2$ @ $\Delta x = 2X_0$ $e \rightarrow \gamma e'$ $E' = E_0/4$

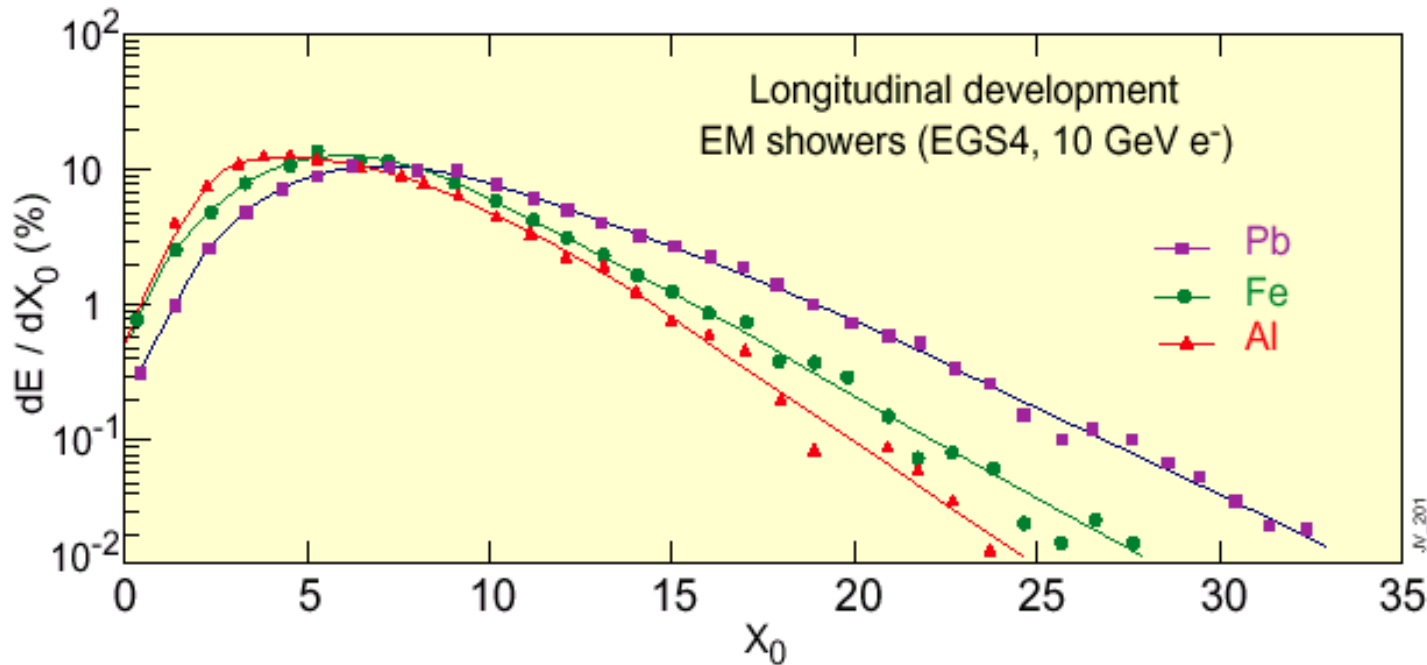
@ $\Delta x = tX_0$ $N(t) = 2^t$ $E(t) = E_0 / 2^t$

@ $t_{\max} X_0$ (shower max) $E(t_{\max}) = E_c$ $E_0 / 2^{t_{\max}} = E_c$

$t_{\max} = \ln(E_0/E_c)/\ln(2)$

$$N_{TOT.} = \sum_{t=0}^{t=t_{\max}} 2^t = 2^{(t_{\max}+1)} - 1 \approx 2 \cdot \frac{E_0}{E_c}$$

EM showers - Longitudinal profile



$$\frac{dE}{dt} \propto t^\alpha e^{-\beta t}$$

Longo e Sestili '75

Parametrization of energy deposition $N_{\text{tot}} \propto E_0/E_c$ $t_{\text{max}} = 1.4 \ln(E_0/E_c)$

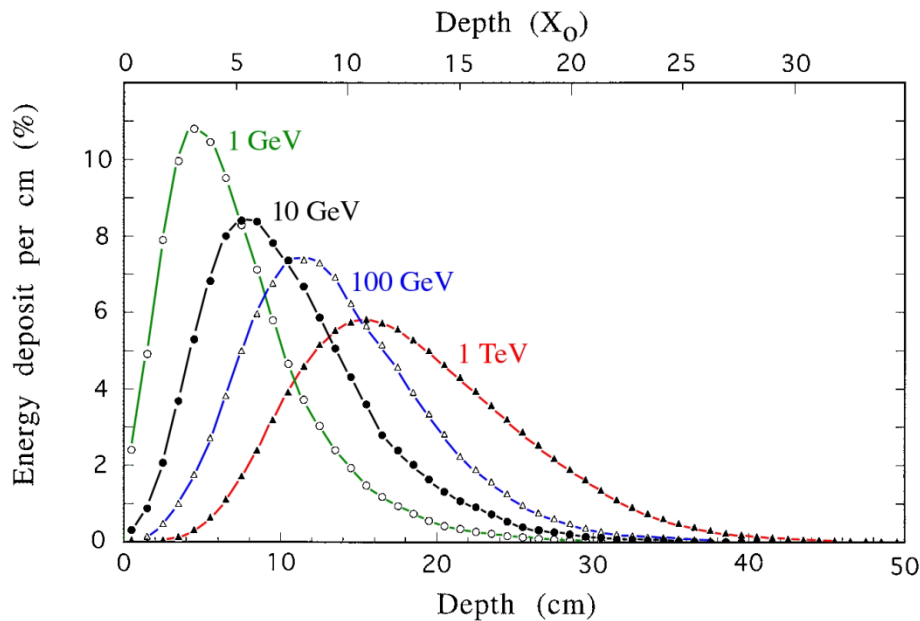
Longitudinal containment $t_{95\%} = t_{\text{max}} + 0.08Z + 9.6$

$E_c \propto 1/Z$ \rightarrow

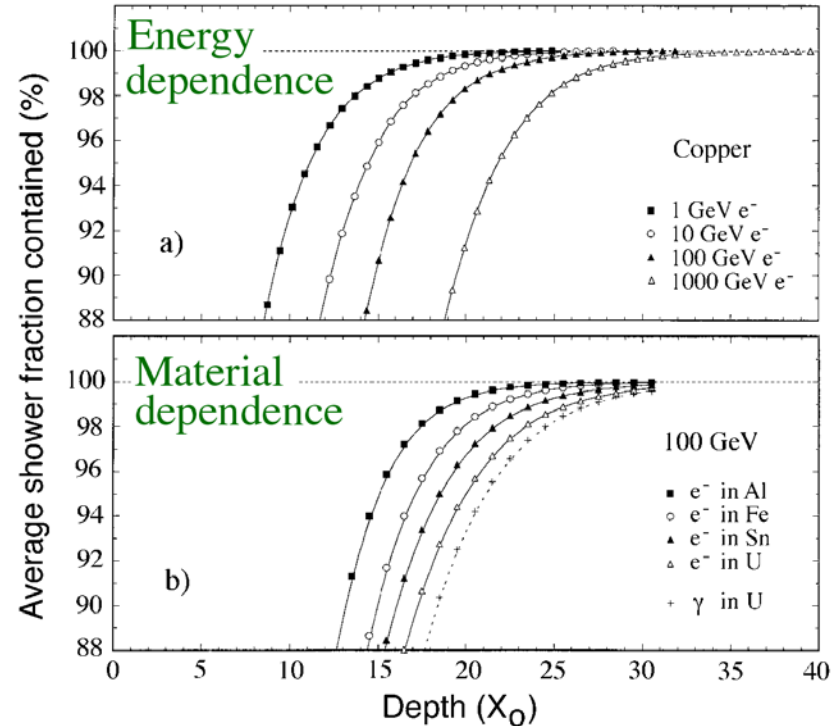
- shower max
- shower tail

EM showers - Longitudinal profile

$$t_{\max} = 1.4 \ln(E_0/E_c)$$



Electron shower in a block of copper



1 GeV electron in copper:
 95% in 11 X_0 and 99% in 16 X_0
 1 TeV electron in copper:
 95% in 22 X_0 and 99% in 27 X_0

EM showers - Parametrizations

Transverse shower profile

- Multiple scattering make electrons move away from shower axis
- Photons with energies in the region of minimal absorption can travel far away from shower axis

Molière radius sets transverse shower size;
on average 90% of the shower is contained within
cylinder of radius R_M around the shower axis.

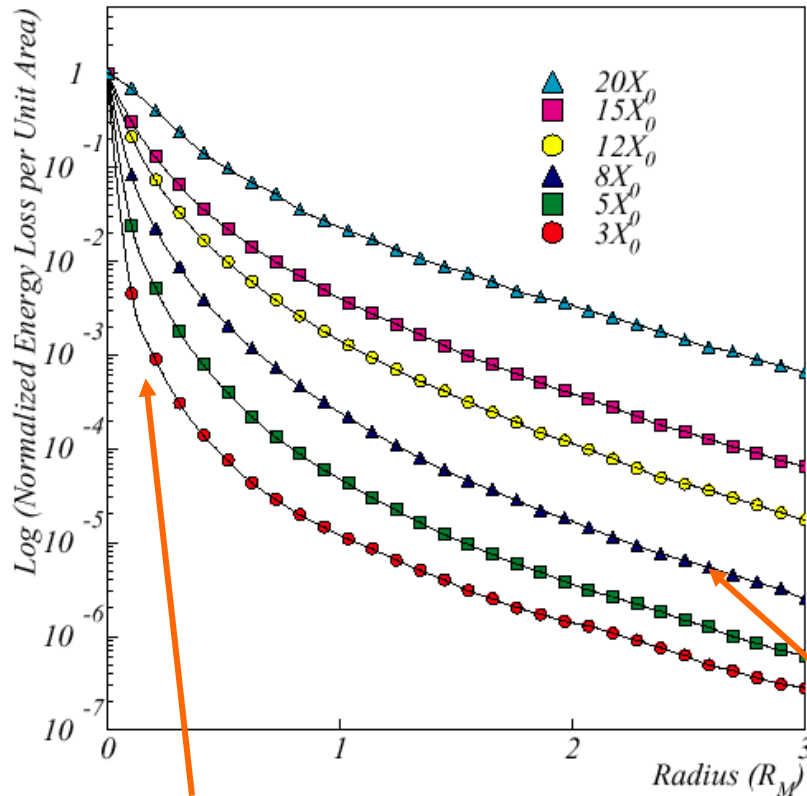
$$R_M = \frac{21 \text{ MeV}}{E_C} X_0$$

$$R_M \propto \frac{X_0}{E_C} \propto \frac{A}{Z} (Z \gg 1)$$

90% E_0 within $1R_M$, 95% within $2R_M$, 99% within $3.5R_M$

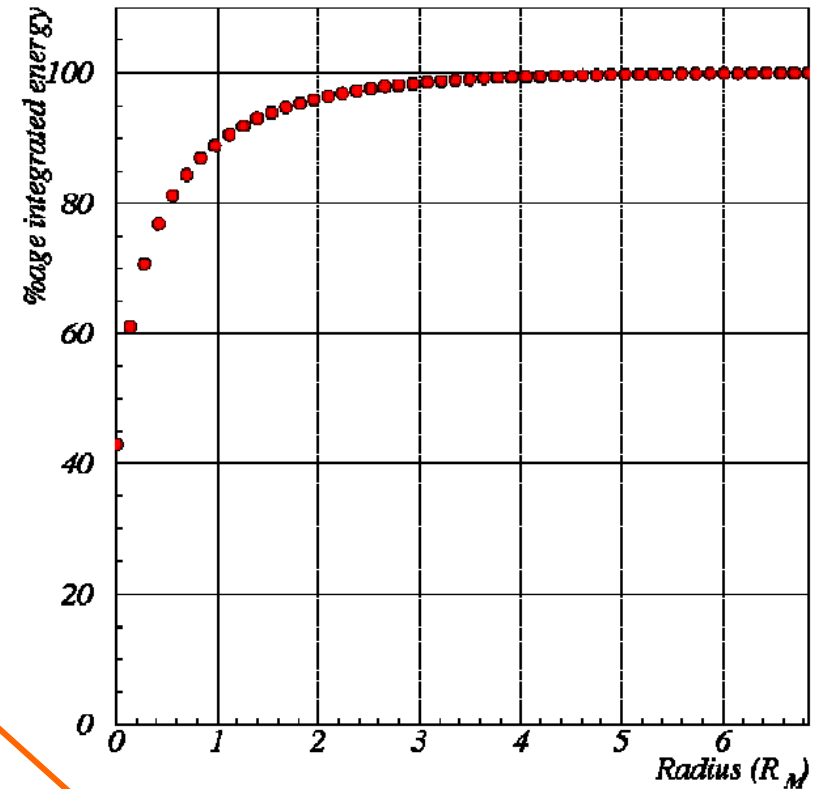
EM showers - Parametrizations

50 GeV electrons in PbWO₄

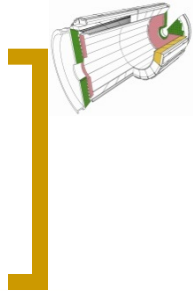


Central core: multiple scattering

50 GeV electrons in PbWO₄

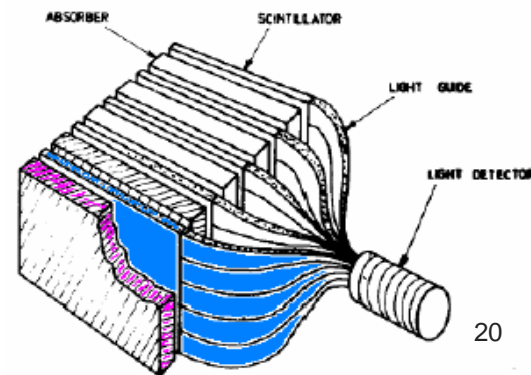


Peripheral halo:
propagation of less attenuated photons,
widens with depth of the shower

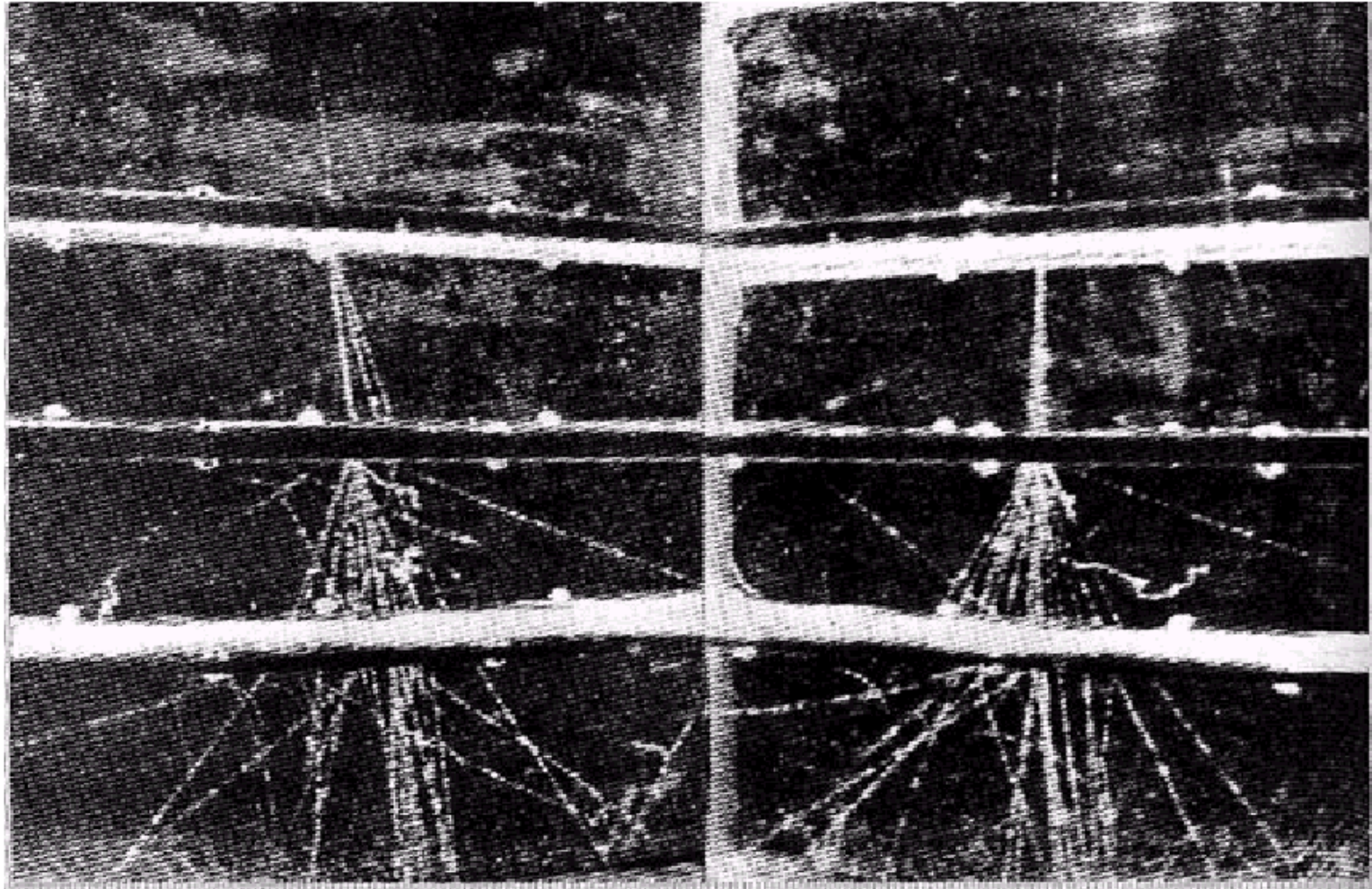


Homogeneous and sampling calorimeters

- In homogeneous calorimeters the absorber and the active medium are the same (e.g. ECAL in Opal, L3, Babar and CMS)
- In sampling calorimeters the two roles are played by two different media (e.g. ECAL in Delphi and Atlas, HCAL in CMS).
 - Shower is sampled by layers of active medium (low-Z) alternated with dense radiator (high-Z) material.
 - Limited energy resolution
 - Detailed shower shape information
 - Reduced cost

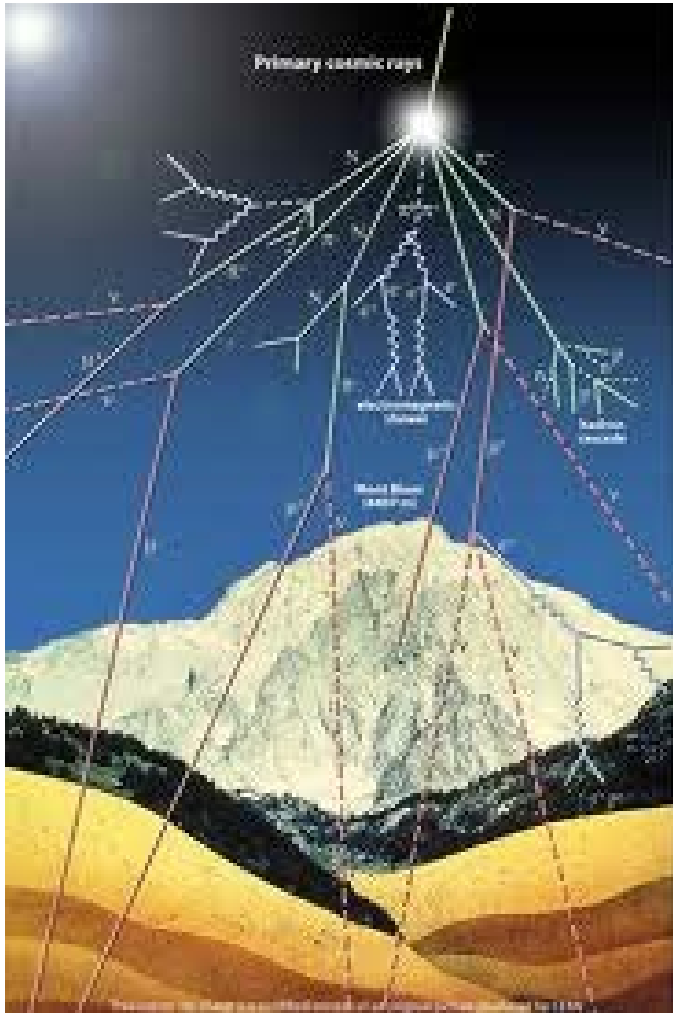


Electromagnetic showers in sampling calorimeter



Cloud chamber photograph of e.m. shower developing in lead plates exposed to cosmic radiation

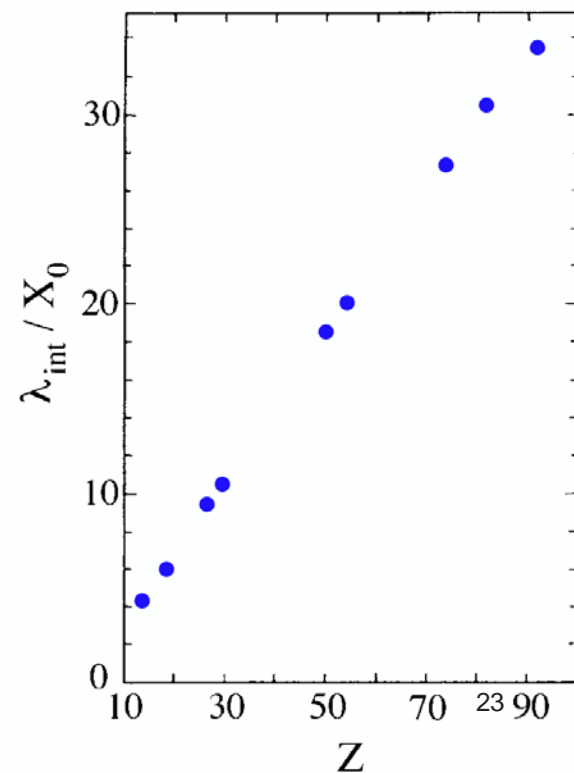
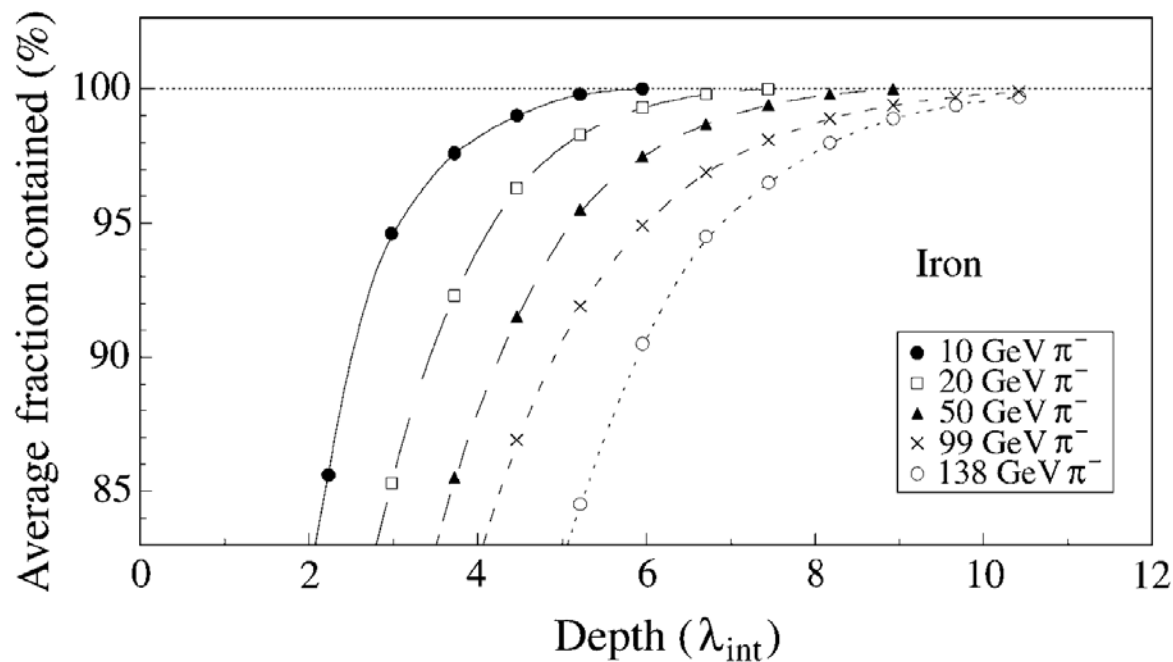
[Hadronic Showers]

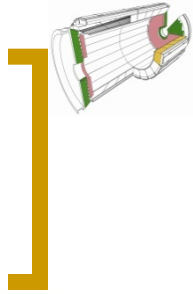


- A very popular hadronic shower.

Hadronic Showers

- Typical scale is the interaction length λ
- Good containment in $\sim 10 \lambda$ but $\lambda > X_0$ (or $\lambda \gg X_0$)
- Larger size of the calorimeters drives the choice of sampling HCAL

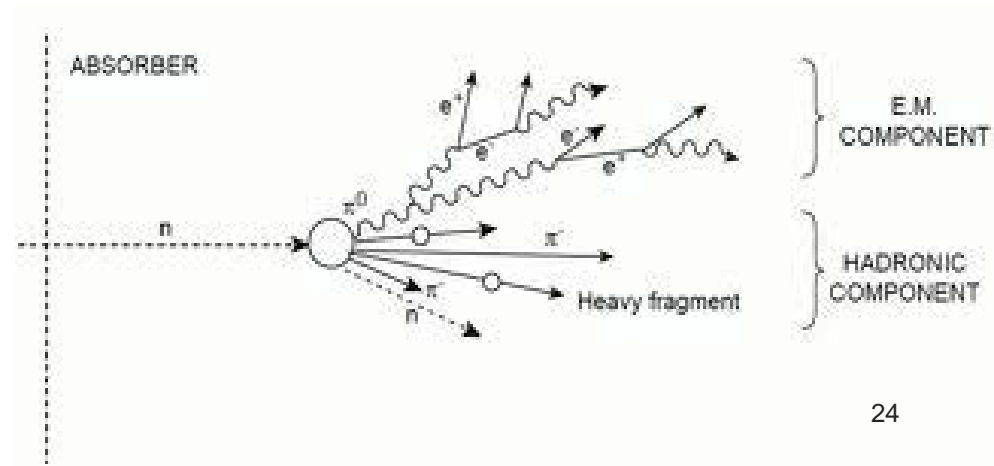




[Hadronic Showers

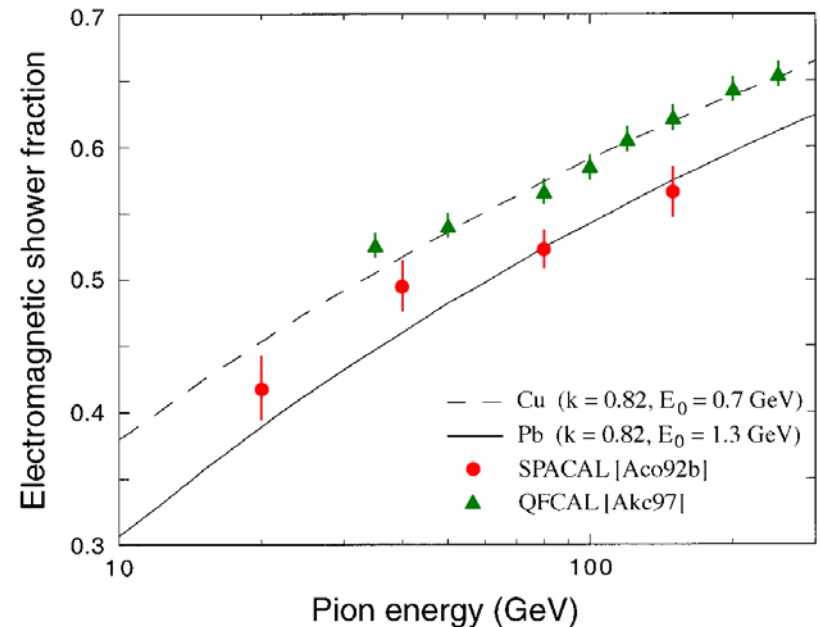
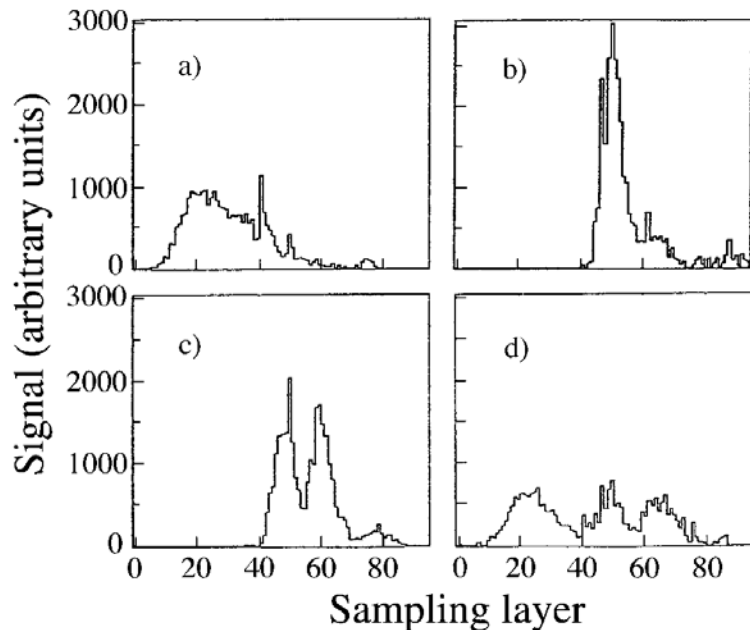
- More complicated than em shower due to the presence of strong interaction.
- Pions (charged and neutral) are by far the most important contribution in the hadronic shower composition but the large majority of the energy is deposited through protons and neutrons.

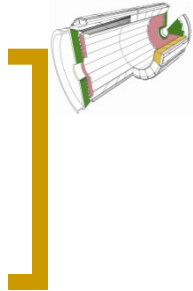
Neutral pions decay in photons before to interact
→ electromagnetic component in the hadronic shower



[Hadronic Showers]

- Big fluctuation in the hadronic shower profile and in the electromagnetic component size.
- Energy dependence of electromagnetic component
- Both the effects strongly affect the calorimeter performance



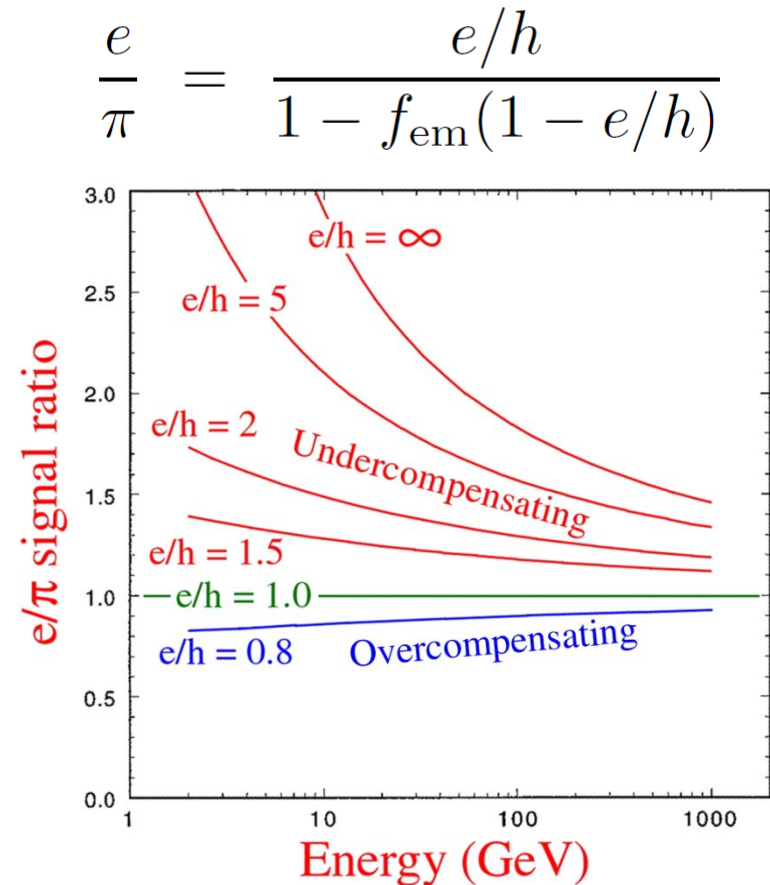
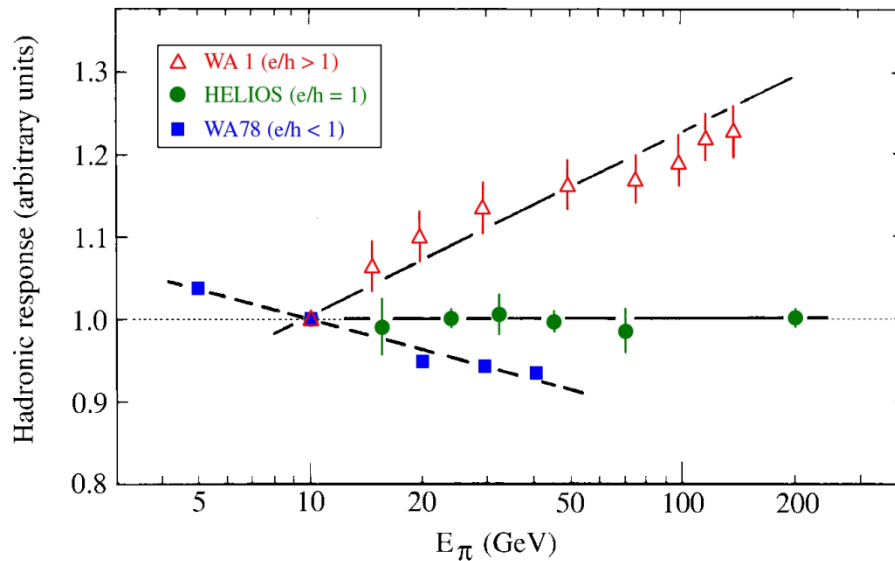


[Hadronic Showers]

- A not negligible fraction of hadronic energy does not contribute to the calorimeter signal ($e/h > 1$):
 - energy to release nucleons from nuclei
 - muons and neutrinos from π/K decays
- The calorimeter response to hadrons is generally smaller than to electrons of the same energy ($\pi/e < 1$).
- Degradation in energy resolution (the energy sharing between em and non-em components varies from one event to another) and linearity (the em fraction of hadron-induced showers increases with energy, so π/e does).

[Compensation]

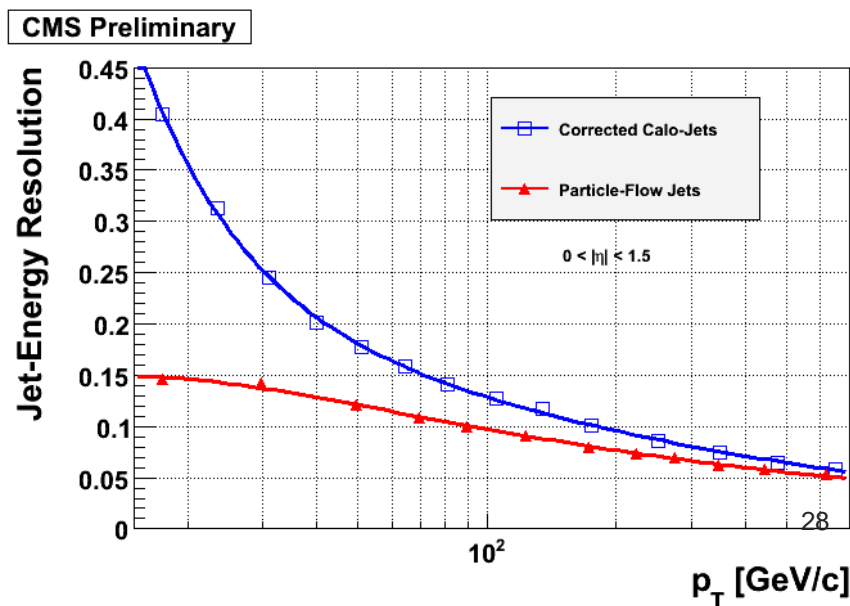
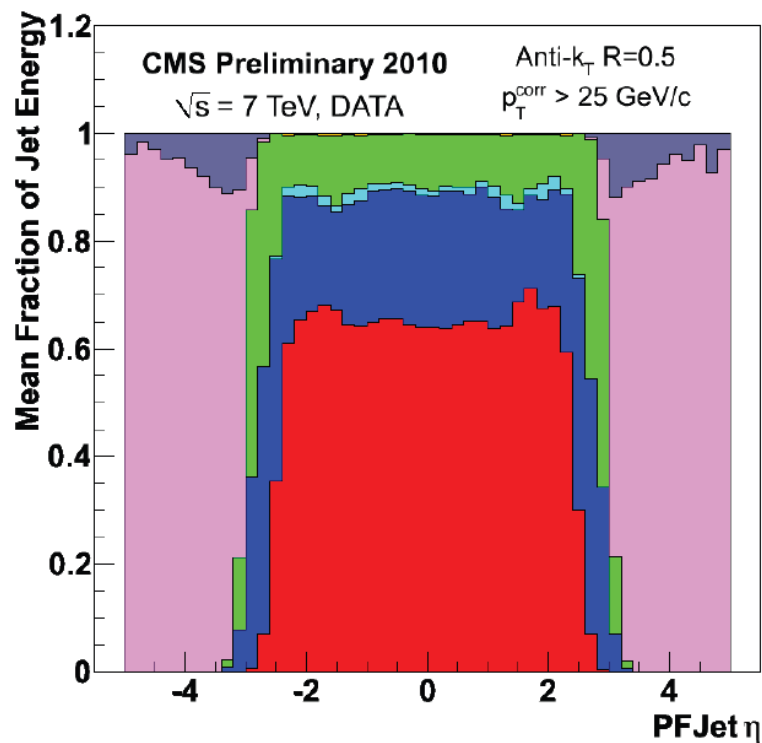
Compensation: equalization of the response to the electromagnetic and non-em shower components ($e/h = 1$).



[Energy Flow]

- Measure charged particles with tracker, photons with ECAL and neutral hadrons with HCAL.
- Fine granularity

Intensively used in CMS
Strong benefit on Jet and
Met resolution.



EM showers - Energy loss detection

The energy deposited in the calorimeters is converted to active detector response

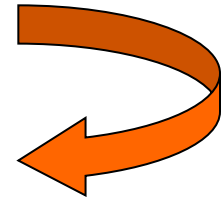
$$\bullet E_{\text{vis}} \leq E_{\text{dep}} \leq E_0$$

Main conversion mechanism

- Cerenkov radiation from e^{\pm}
- Scintillation from molecules
- Ionization of the detection medium

response \propto total
track length

Different energy threshold E_s for
signal detectability



Scintillators

Luminescent materials emit light when stimulated with light and heat (photo-luminescence) and radiation (scintillation).

Two classes: organic and inorganic scintillators.

Inorganic (crystalline structure)

Up to 40000 photons per MeV

High Z

Large variety of Z and ρ

Undoped and doped

ns to μ s decay times

Expensive

E.m. calorimetry (e, γ)

Medical imaging

Fairly Rad. Hard (100 kGy/year)

Organic (plastics or liquid solutions)

Up to 10000 photons per MeV

Low Z

$\rho \sim 1 \text{ gr/cm}^3$

Doped, large choice of emission wavelength

ns decay times

Relatively inexpensive

Tracking, TOF, trigger, veto counters,
sampling calorimeters.

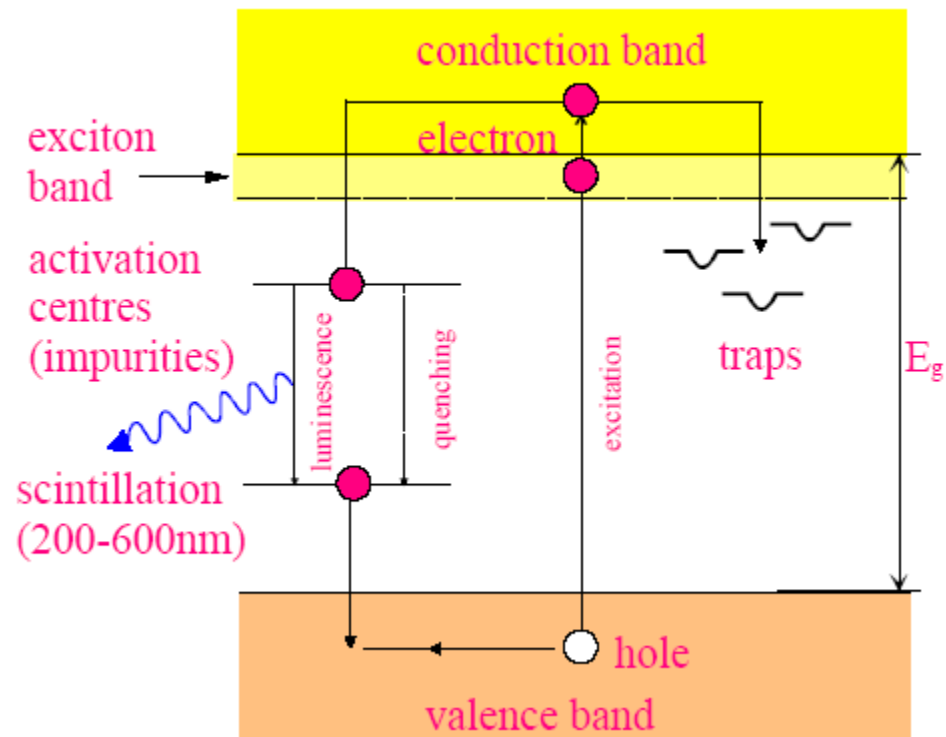
Medium Rad. Hard (10 kGy/year)

Scintillation mechanism

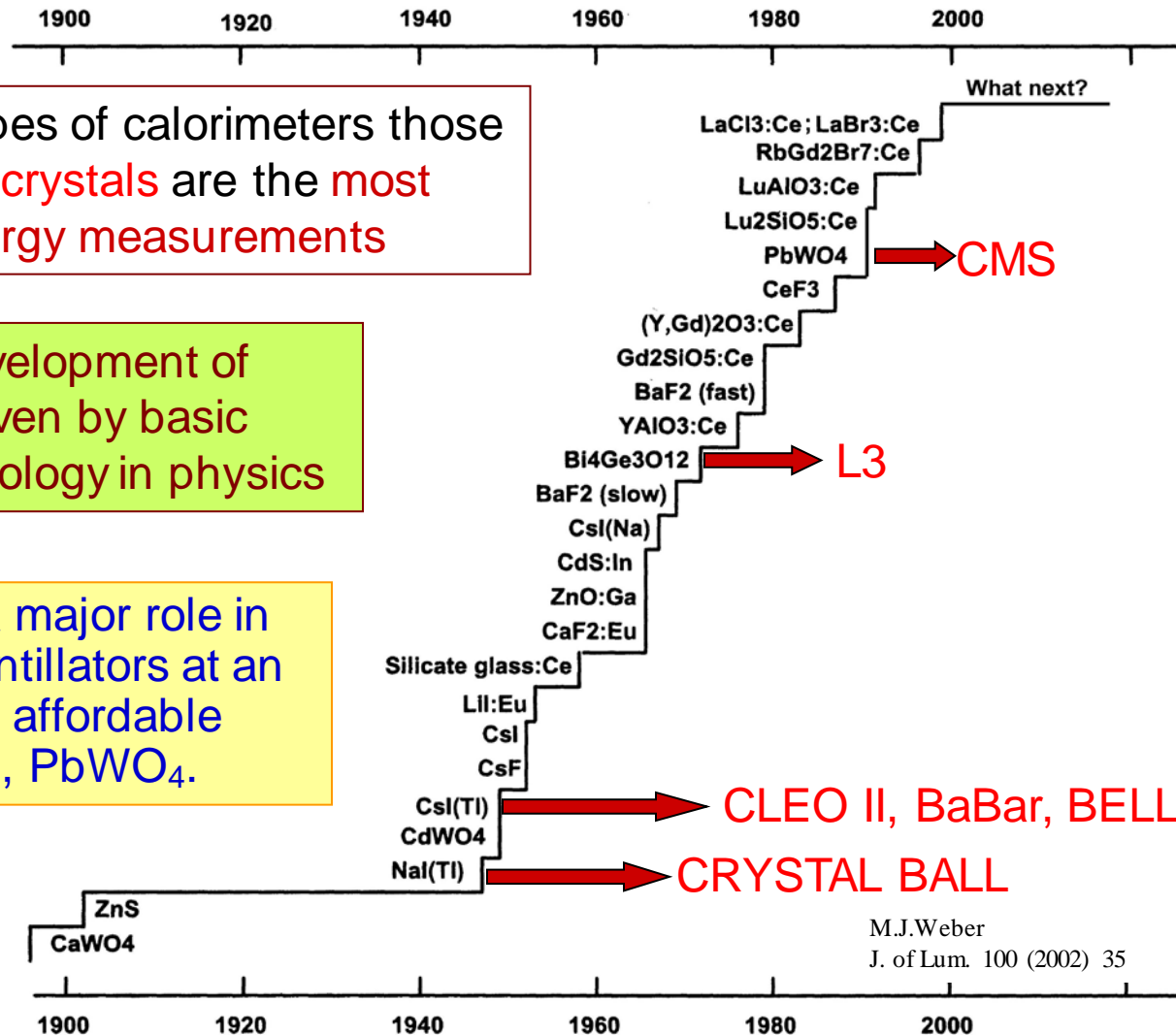
Scintillators need impurities (dopant) in order to emit at a different wavelength and not reabsorb the light.

The centres are of three main types:

- **Luminescence centres**
photon emission
- **Quenching centres**
thermal dissipation of the excited energy
- **Traps**
metastable levels, from where electrons may subsequently go to
 - conduction band by thermal energy
 - valence band by a radiationless transition

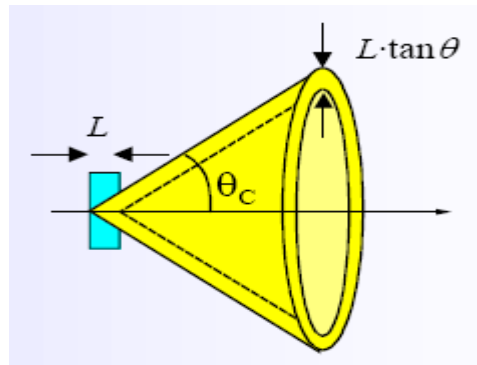
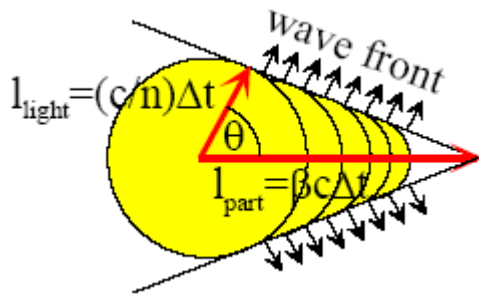


Scintillating Crystal History



Cherenkov Light

- A charged particle traveling in matter with speed greater than c/n (the speed of the light in the same material) emits photons mainly in the visible (mainly in the blue).



Maximum value for the emission angle ($v=c$)

$$\theta_{\text{max}} = \arccos \frac{1}{n}$$

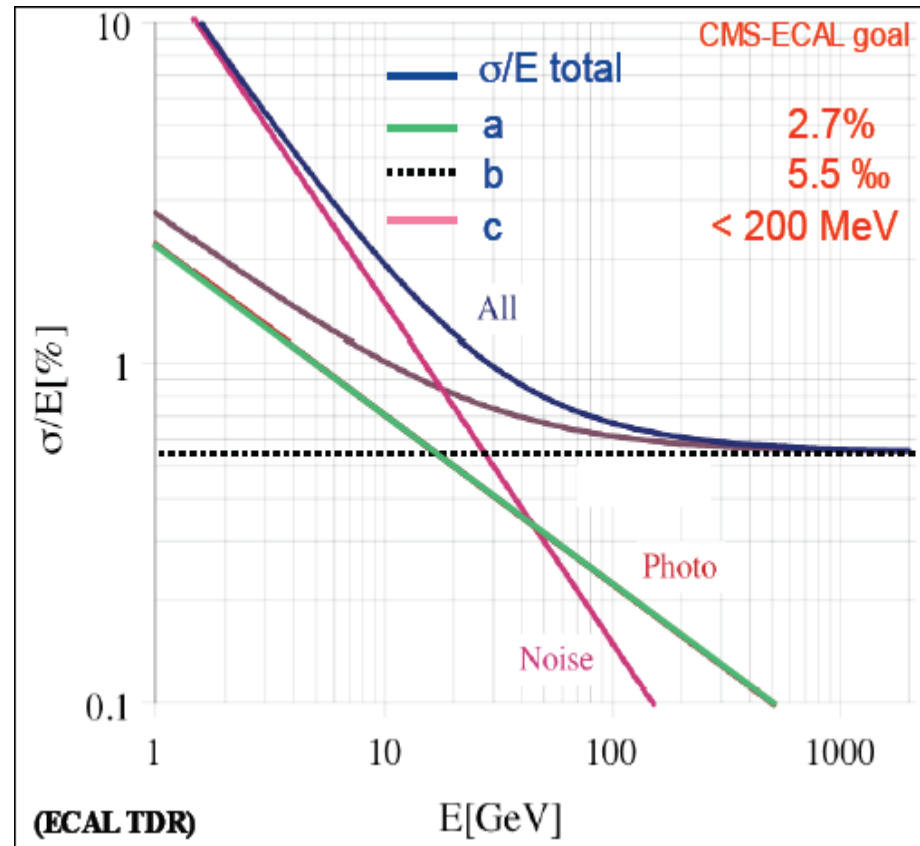
- The energy loss by Cherenkov effect is much smaller than the energy loss by ionization: high gain photodetector is needed (e.g. PMTs)

Energy Resolution (1)

$$\frac{\sigma}{E} = \frac{s}{\sqrt{E}} \oplus c \oplus \frac{n}{E}$$

\oplus means quadratic sum

- **S**: stochastic term from Poisson-like fluctuations
 - sampling contribution dominant in sampling calorimeters
- **c**: constant term
 - dangerous limitation to high energy resolution
 - important contribution from intercalibration constants
- **n**: noise term from electronic and pile-up
 - relevant at low energy



Energy Resolution (2)

- **S: stochastic term from Poisson-like fluctuations**

(natural advantage of homogenous calorimeters; s can be ~ 2%-3%)

- photostatistics contribution:
 - light yield
 - geometrical efficiency of the photodetector
 - photocatode quantum efficiency



$$E \propto N_{\text{p.e.}}$$

$$\sigma(N_{\text{p.e.}}) \propto \sqrt{N_{\text{p.e.}}}$$

$$\Rightarrow \frac{\sigma(E)}{E} \propto \frac{1}{\sqrt{E}}$$

Including gain fluctuations of photo-detector (F):

$$\frac{\sigma(E)}{E} = \sqrt{\frac{F}{N_{\text{p.e.}} \cdot E}}$$

$F = 2 - 3; N_{\text{p.e.}} \geq 4000/\text{GeV}$

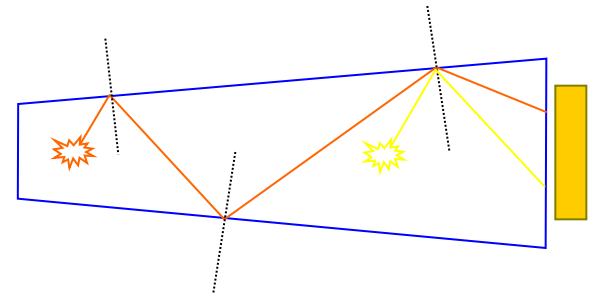
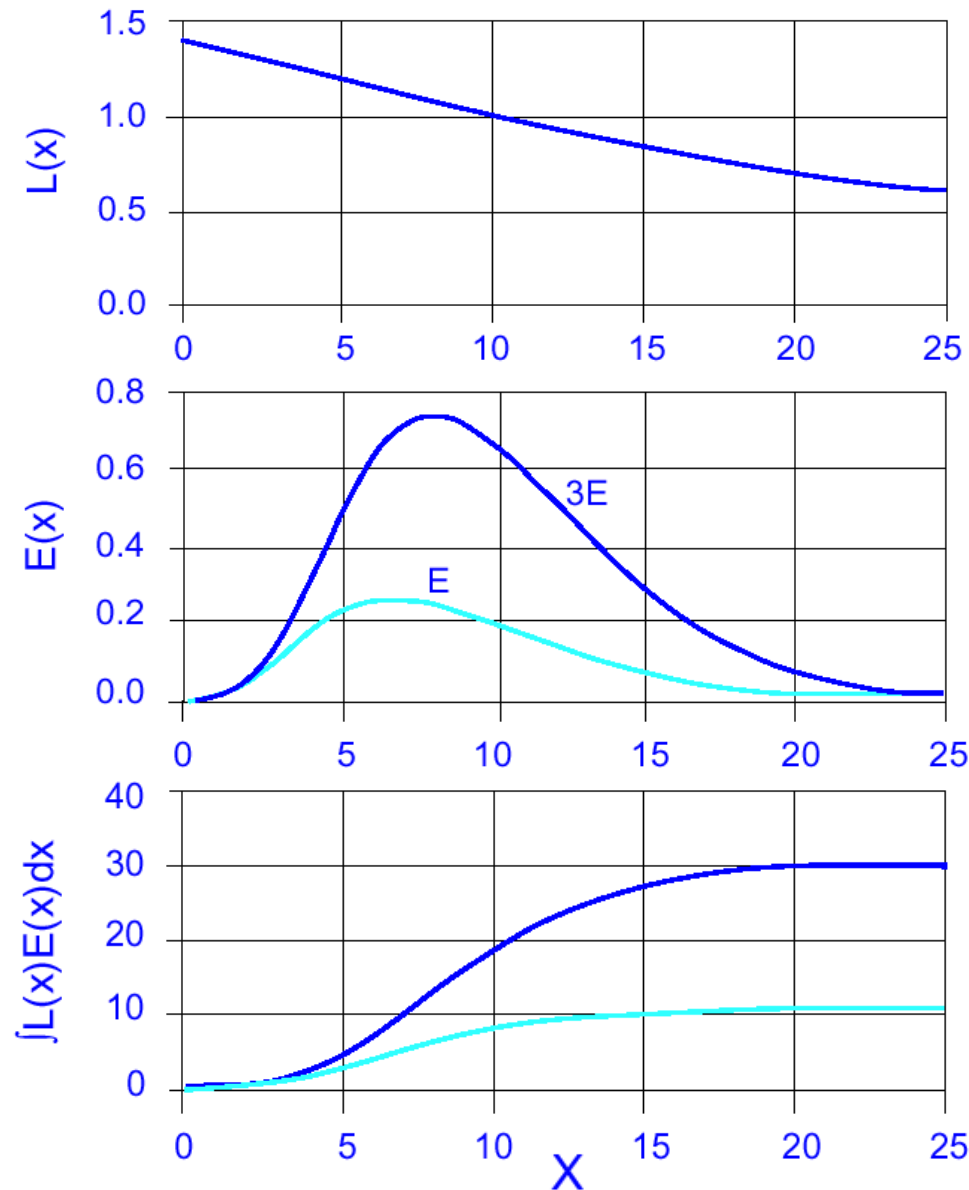
- electron current multiplication in photodetector
- lateral containment of the shower
- Material in front of the calorimeter

Energy Resolution (3)

Constant Term contributions in CMS ECAL:

- leakage (front, rear, dead material)
- temperature stabilization $< 0.1\text{ }^{\circ}\text{C}$
($dLY/dT = -2.0\%/^{\circ}\text{C}$ @ 18°C ;
 $dM/dT \sim -2.3\%/^{\circ}\text{C}$)
- APD bias stabilization ($\pm 20\text{ mV}$ / 400 V)
($dM/dV = 3\%/V$)
- light collection uniformity
- intercalibration by light injection monitor and physics signals

Light Collection Uniformity



- non linearity of the response (can be corrected)
- smearing of the response at fixed energy due to shower fluctuations (can not be corrected)

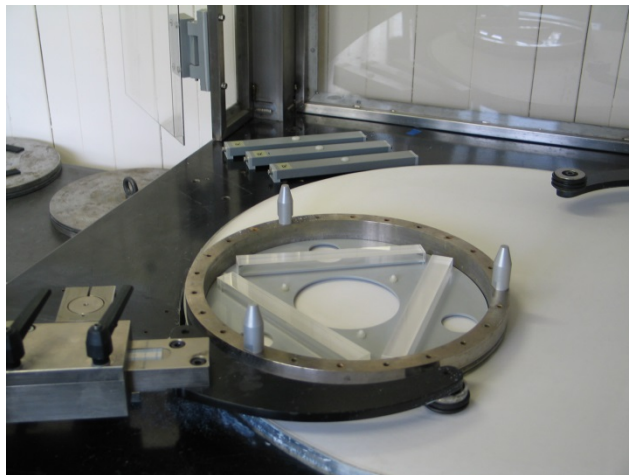
$$\int_0^x L(x)E(x)dx$$

ratio 2.89
(instead of 3)

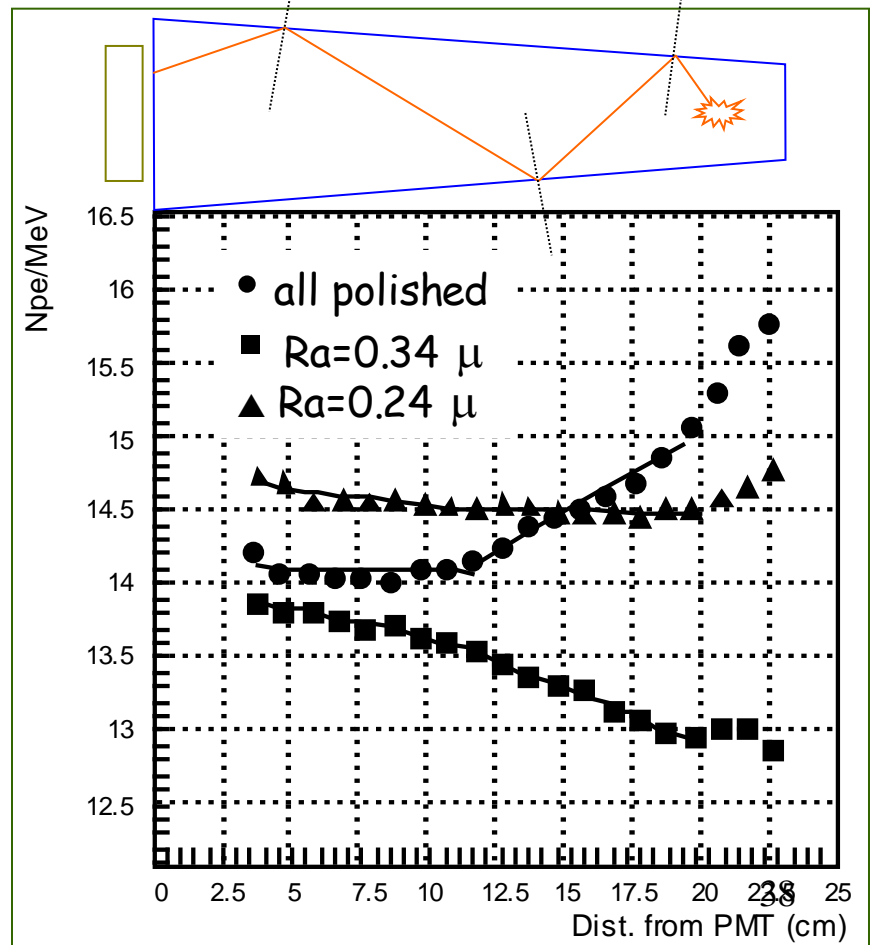
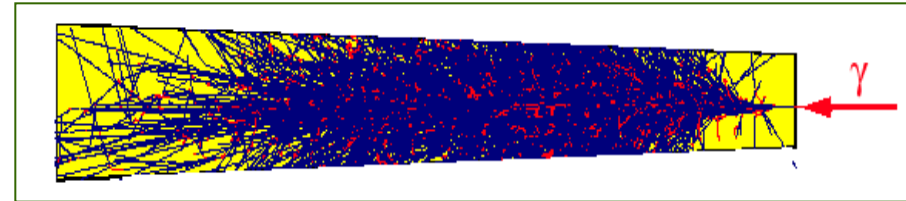
Light Collection Uniformity

- High refractive index make light collection difficult
- Focusing effect due to tapered shape of barrel crystals
- Uniformity can be controlled by depolishing one lateral face with a given roughness

Uniformity treatment



Riccardo Paramatti



The CMS calorimeters

Disclaimer: due to the limited time, I selected few “ECAL oriented” examples to show the performance in CMS.

Plots from the CMS
paper EGM-11-001

<http://m.iopscience.iop.org/1748-0221/8/09/P09009>

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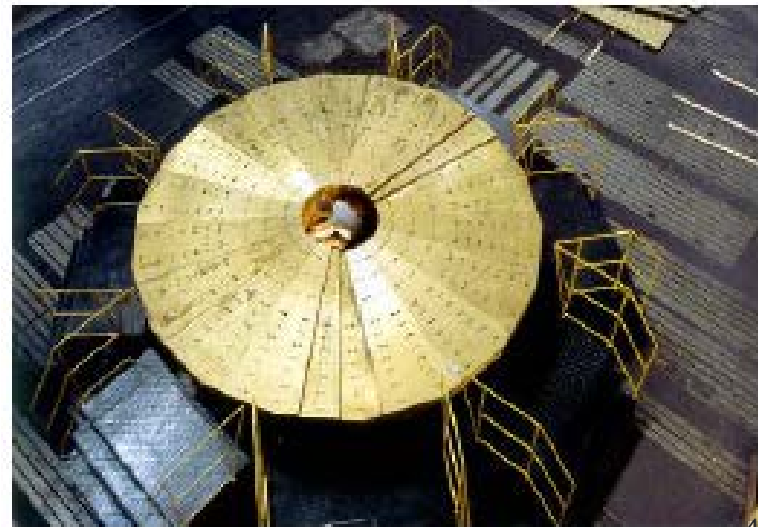
ACCEPTED: August 8, 2013

PUBLISHED: September 19, 2013

**Energy calibration and resolution of the CMS
electromagnetic calorimeter in pp collisions at
 $\sqrt{s} = 7$ TeV**

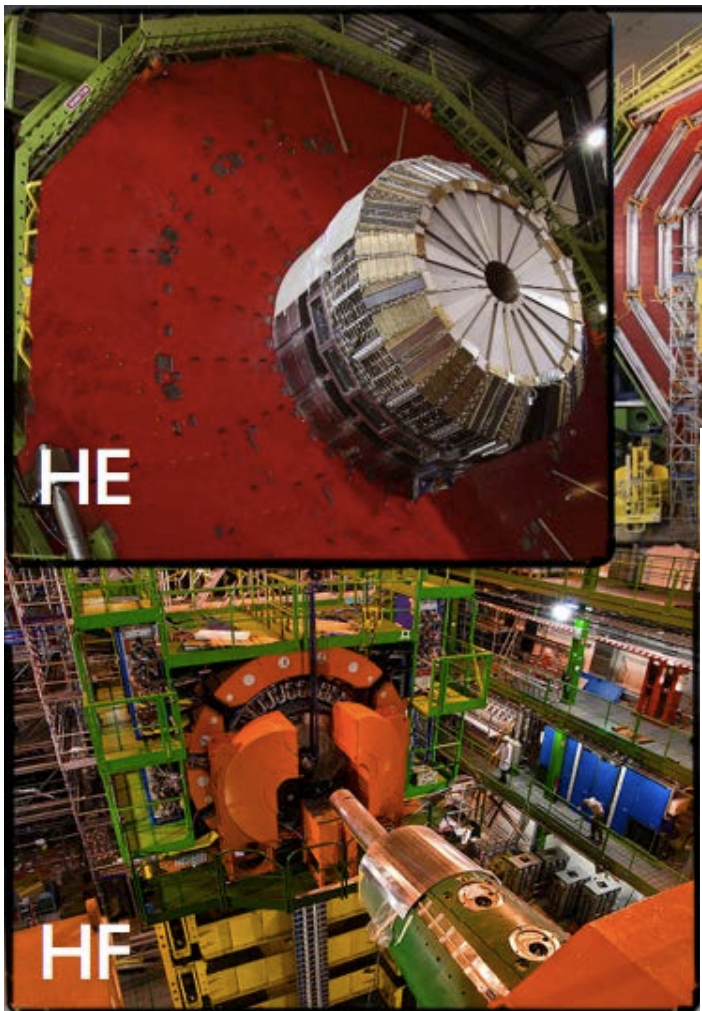
CMS Hadronic Calorimeter

- Hadronic Barrel (HB) and Endcap (HE) calorimeters:
 - sampling brass/plastic scintillator tiles
 - HO: additional scintillator layer outside the solenoid cryostat
- The forward calorimeter (HF):
 - steel and quartz fiber covers up to $|\eta| < 5.2$

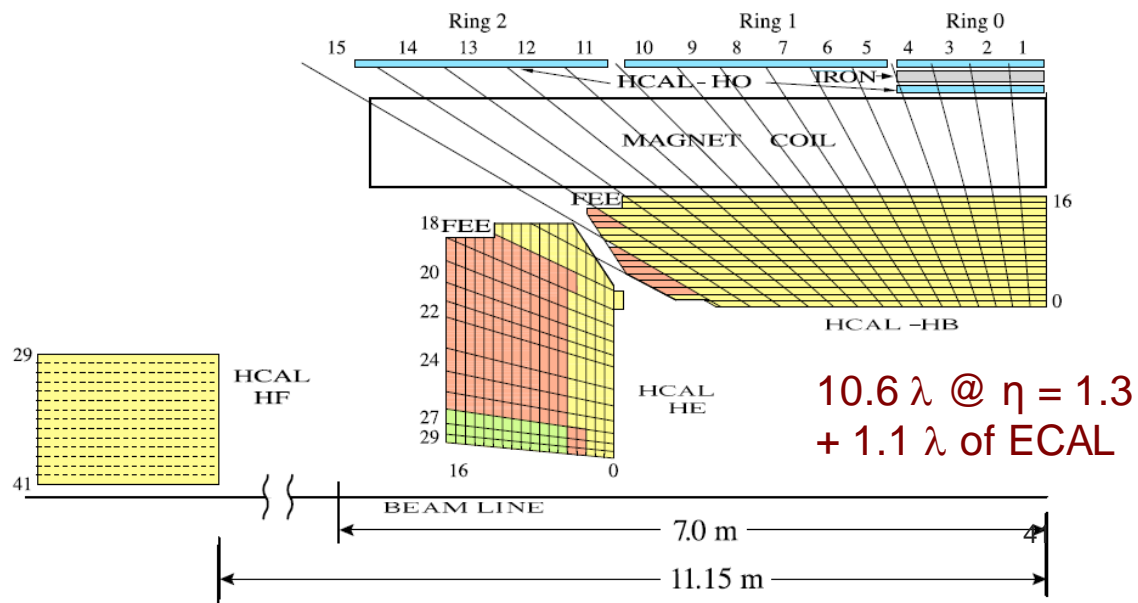


- old russian shell casings recycled for brass !

CMS Hadronic Calorimeter

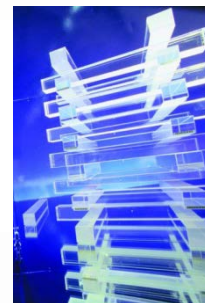
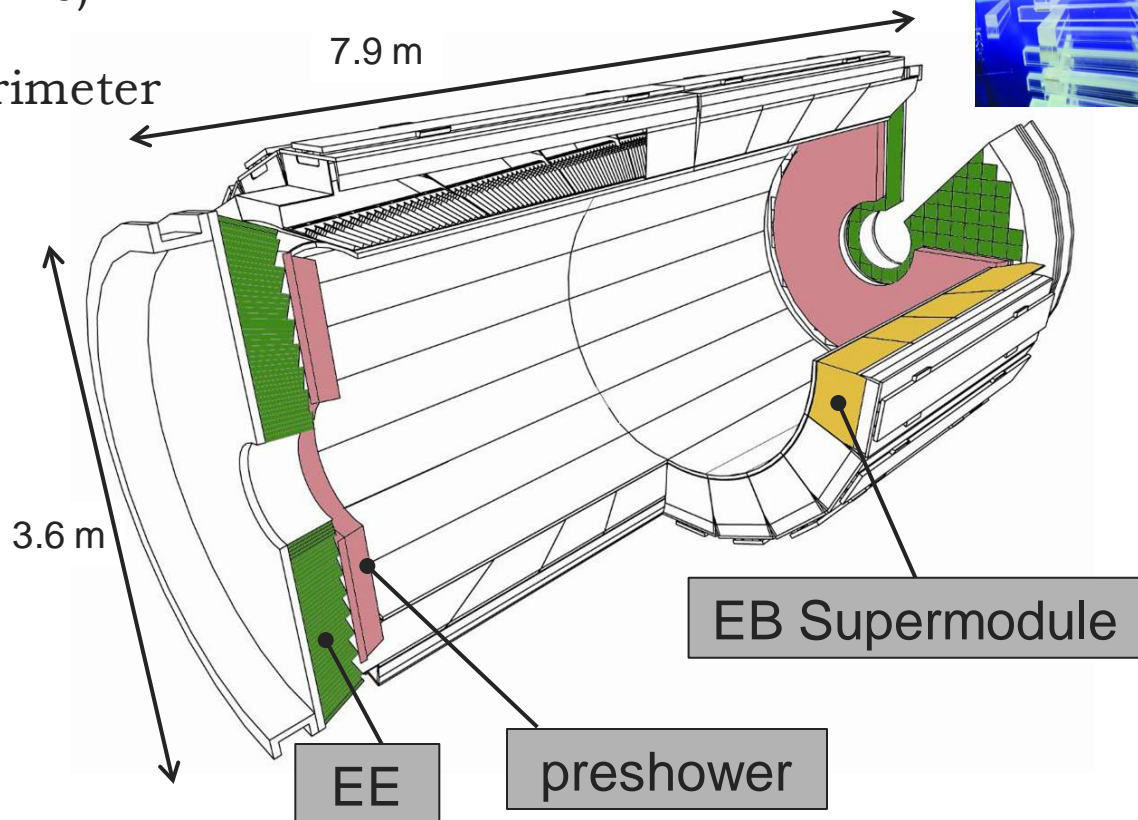


Detector	Readout	# Channels
HB/HE/HO	Hybrid Photo-Diode (HPD)	2592/2592/2160
HF	PMT	1728



CMS Electromagnetic Calorimeter

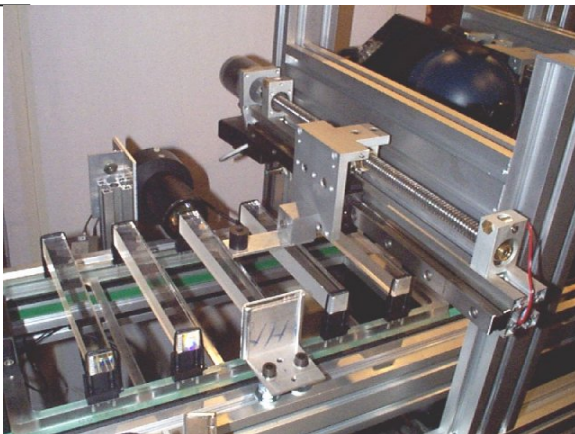
- Excellent energy (and position) resolution for photons and electrons ($H \rightarrow \gamma\gamma$, $H \rightarrow ZZ \rightarrow 4e$)
- Lead Tungstate (PbWO_4) homogenous crystal calorimeter
- Barrel (EB):
 - 36 Supermodules (SM), each 1700 crystals
 - $|\eta| < 1.48$
 - APD photodetectors
- Endcaps (EE):
 - 2 Endcap sides, each 7324 crystals
 - $1.48 < |\eta| < 3.0$
 - VPT photodetectors
- Preshower (ES):
 - sampling calorimeter (lead, silicon strips)
 - $1.65 < |\eta| < 2.6$



Pre-calibration Campaign

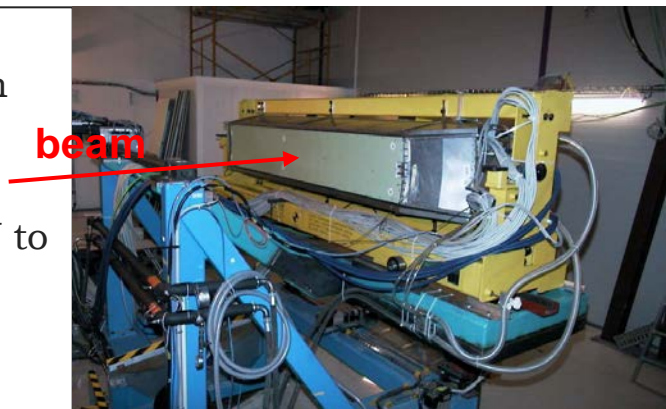
A very intense 10 years long pre-calibration campaign. Several orders of magnitude in energy: from 1 MeV of Co^{60} source to 120 GeV electron beam.

Laboratory measurements during crystal qualification phase.
(2000-2006)



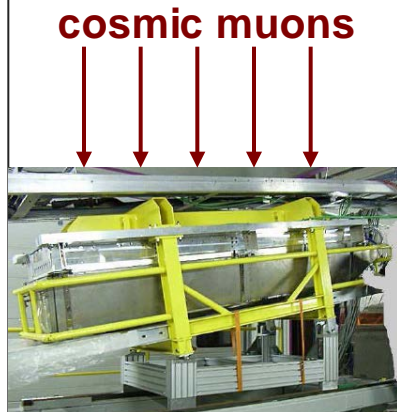
Test Beam:
Cern electron beams.

From 15 GeV to 250 GeV.
(2004-2007)

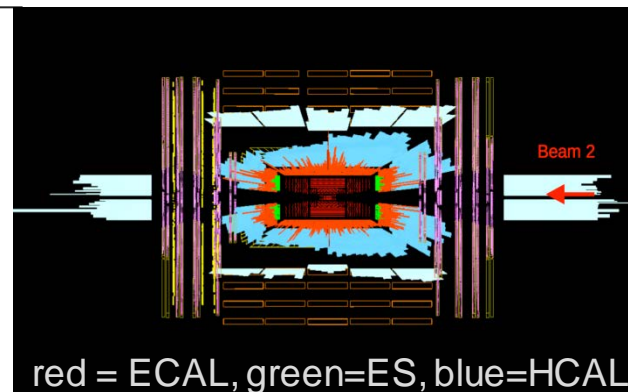


Channel intercalibration with cosmic muons (only Barrel SMs)

(2006-2007)



Beam Splash:
In September 2008 and November 2009, beam was circulated in LHC, stopped in collimators 150m away from CMS

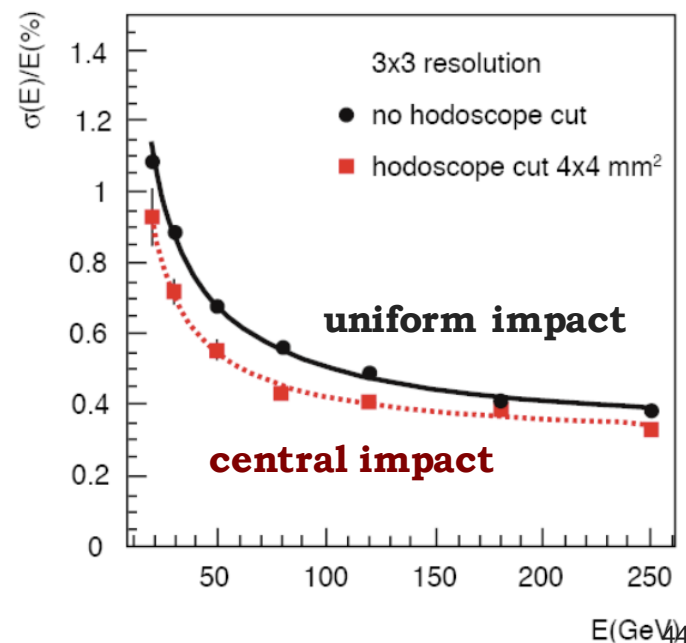


Energy resolution challenge

- ECAL «standalone» energy resolution measured at the test beam:
(3x3 arrays of barrel crystals in the absence of magnetic field, with no material in front of the calorimeter and negligible inter-calibration contribution in the constant term)

$$\frac{\sigma(E)}{E} = \frac{2.8\%}{\sqrt{E(\text{GeV})}} \oplus \frac{0.128}{E(\text{GeV})} \oplus 0.3\%$$

- Results used to tune MC simulation.
- In-situ, for unconverted photons with energies in the range of interest for physics analyses, ~100 GeV, the in-situ constant term dominates.
- Constant term in-situ strongly depends on the quality of the stability, calibration and monitoring.
- Asymptotically to be kept at ~0.5%

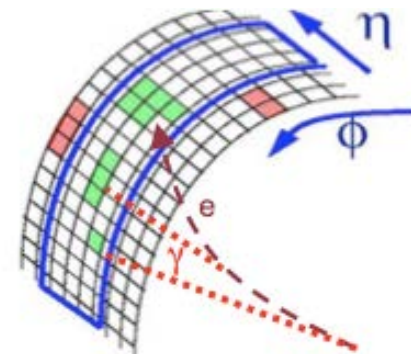


[e/γ energy with ECAL]

Measurement of electron/photon energy:

$$E_{e,\gamma} = F_{e,\gamma} \cdot \sum_{xtal} (G \cdot C_{xtal} \cdot L_{xtal}(t) \cdot A_{xtal})$$

- A_{xtal} [ADC counts] → signal channel amplitude
- L_{xtal} → laser monitoring correction (time dependent)
- C_{xtal} → crystal inter-calibration ($\langle C_{xtal} \rangle = 1$)
- G [GeV/ADC] → ECAL energy scale
- Σ → e.m. shower, energy deposited over several crystals clustered with dynamic algorithms
- F → cluster energy corrections
 - particle dependent
 - compensate shower leakage and bremsstrahlung losses for electrons)

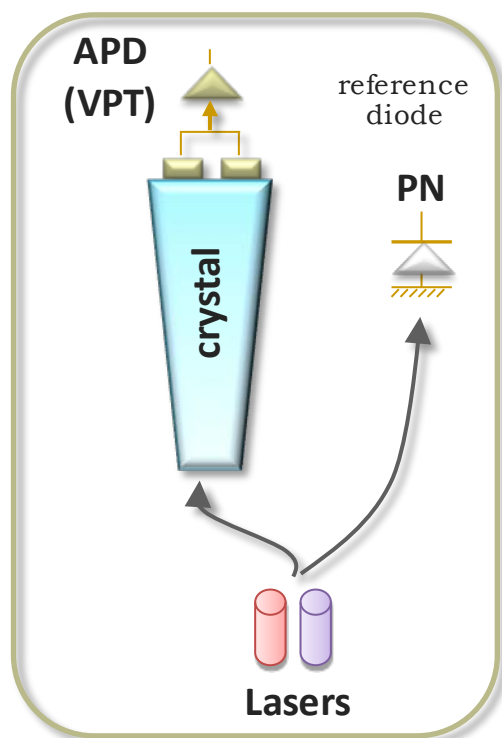


ECAL response monitoring

Radiation \rightarrow Wavelength-dependent loss of light transmission (w/o changes in scintillation)

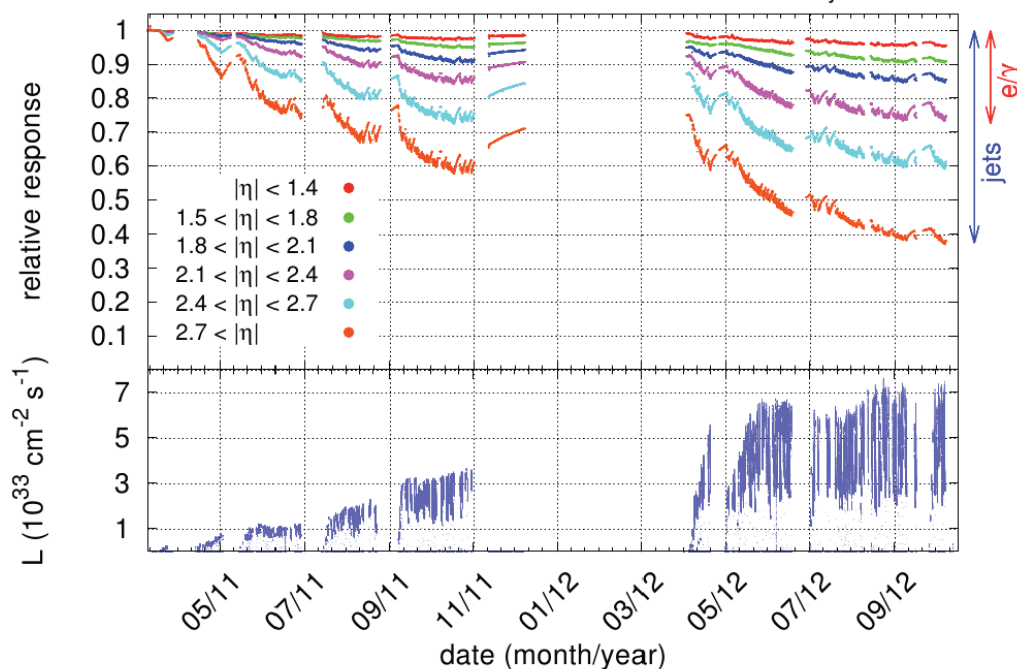
Crystal Transparency **drops** within a run by a few percent but **recovers** in the inter-fill periods

- Inject fixed amount of light to monitor transparency loss
- Response loss up to 5% in EB and up to 60% in EE (25% in the electron acceptance region $|\eta| < 2.5$)

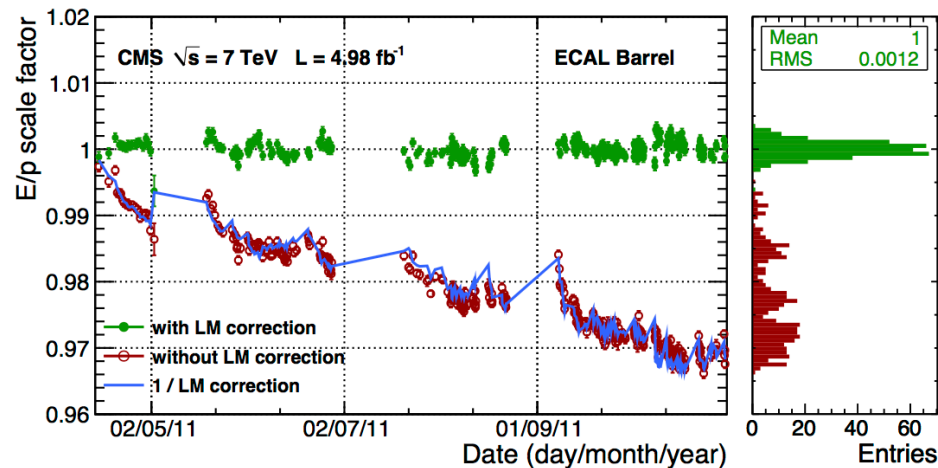


Cycle of response loss during irradiation and recovery in beam-off periods

CMS Preliminary 2011-2012



ECAL response stability

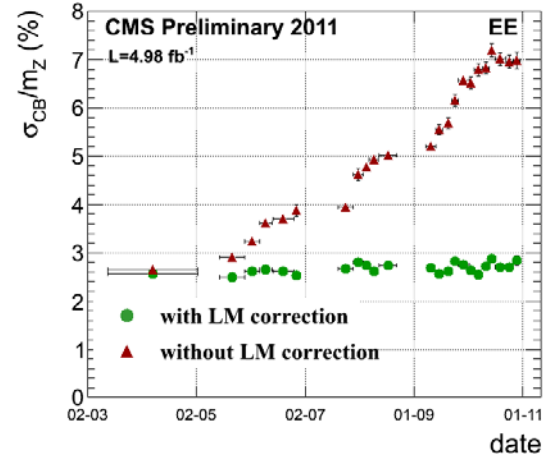
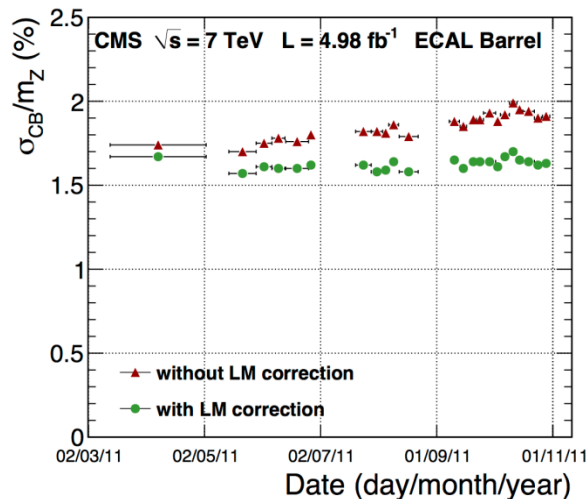


Stability (2011) of the energy scale after monitoring corrections with W_{ev} events.

- Barrel: average signal loss $\sim 2.5\%$
RMS stability $\sim 0.12\%$
- Endcaps: average signal loss $\sim 10\%$
RMS stability $\sim 0.35\%$

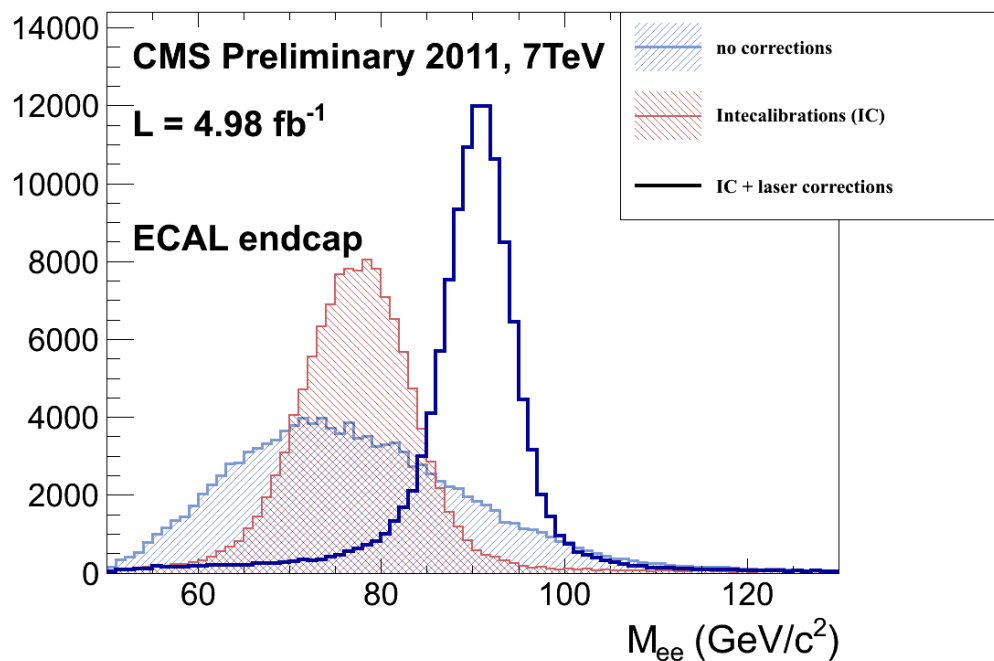
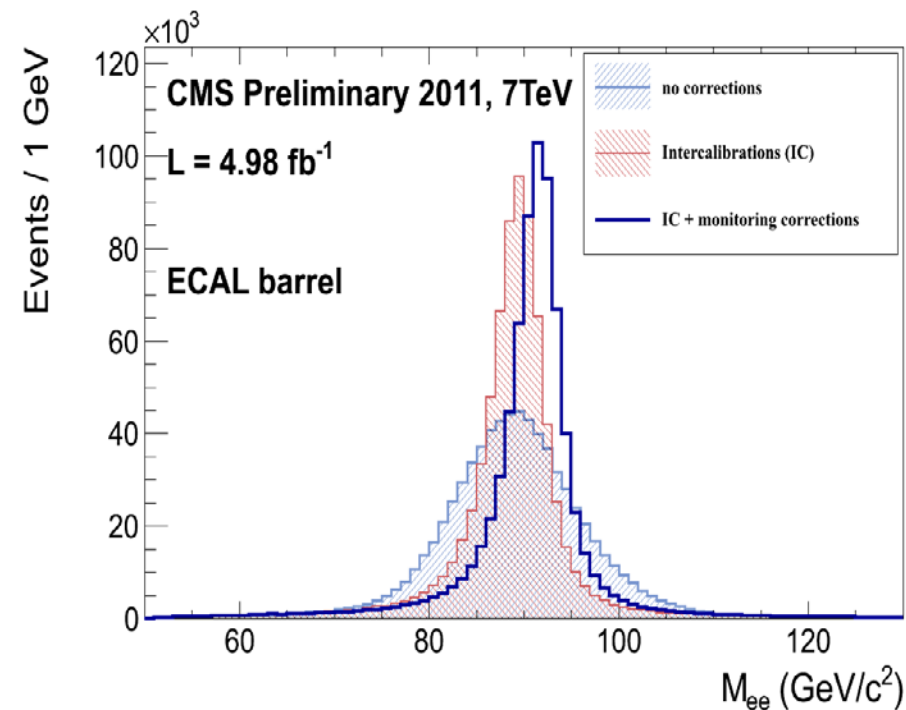
Stability of the ECAL resolution from Zee invariant mass peak.

- Barrel: resolution stable within errors.
- Endcaps: worsening of $\sim 1.5\%$ in quad. (residual PU effect)



ECAL Calibration

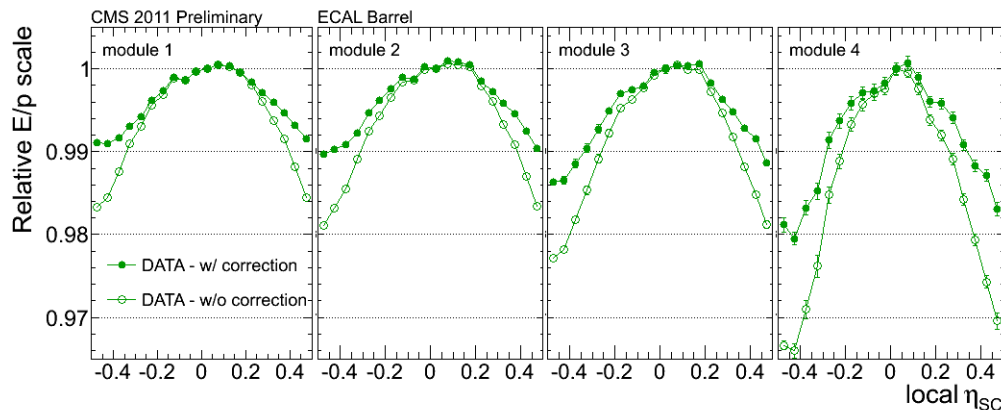
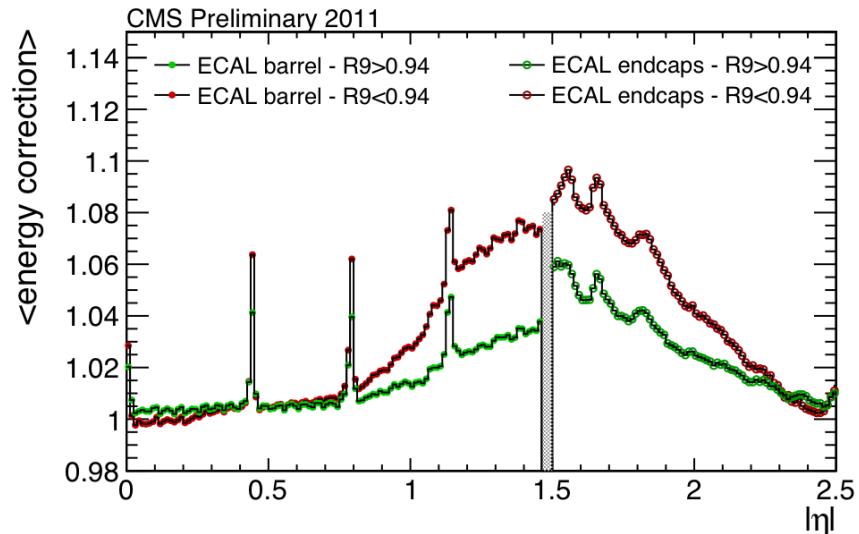
- Zee invariant mass distribution applying :
 - channel Inter-Calibration
 - IC and Laser Monitoring corrections



Cluster Energy Corrections

Cluster Energy corrections vs pseudo-rapidity for **non-showering** and **showering** electrons.

- compensate for unclustered energy and energy not reaching the calorimeter: strongly related to the amount of material in front of ECAL.
- energy lost inside gaps: intermodule boundary visible in the Barrel

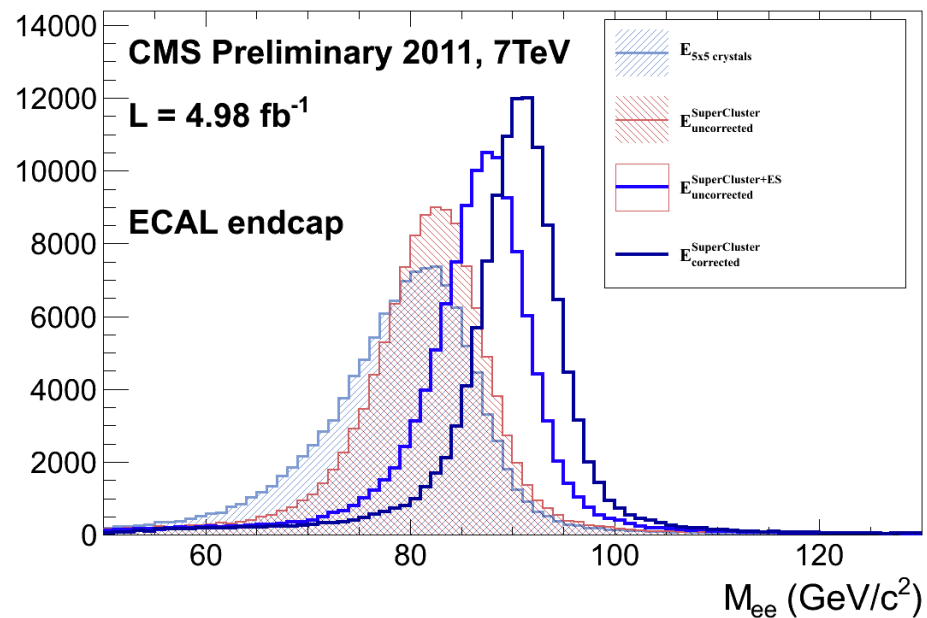
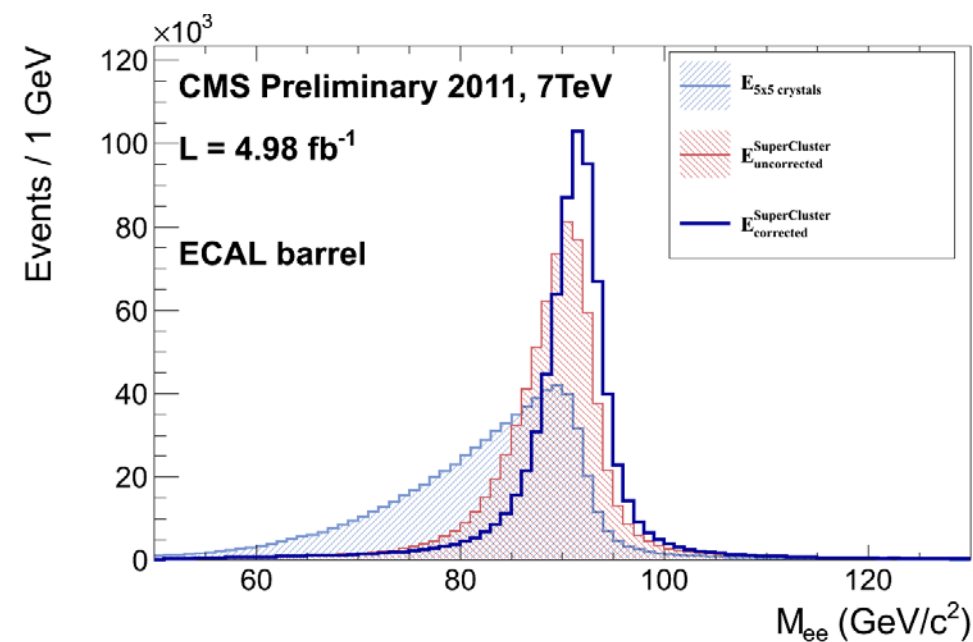


Reconstructed energy as a function of the local position of the most energetic crystal in the cluster, with E/p method.

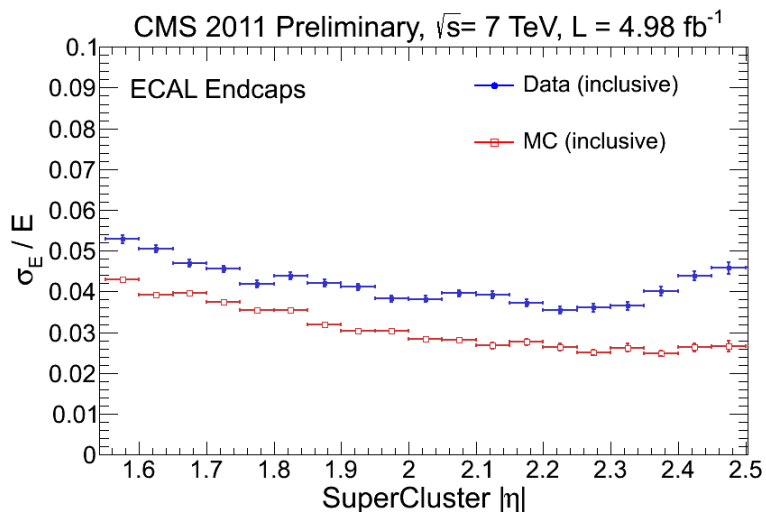
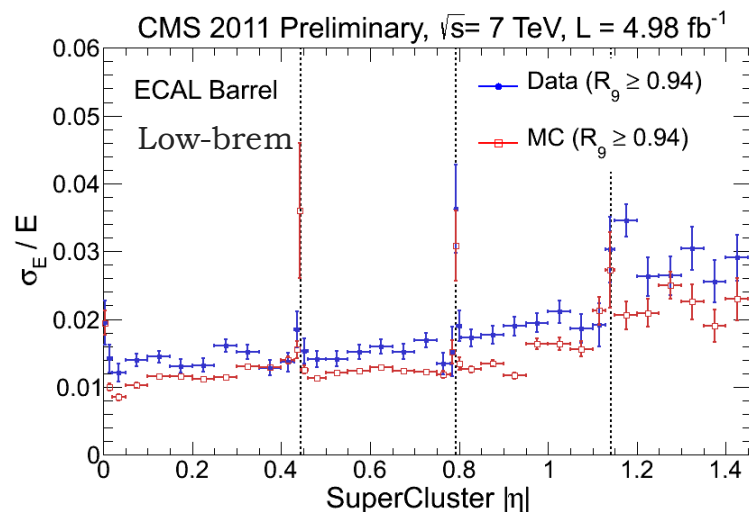
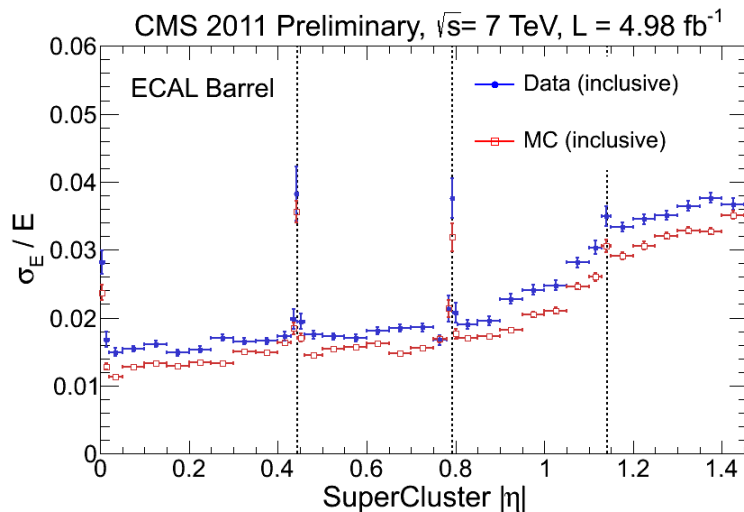
- MC driven corrections not sufficient to correct the data
- crystal staggering variation along η (bigger in module 4)

Optimal clustering

- Zee invariant mass distribution with optimal ECAL clustering



Z electrons energy resolution

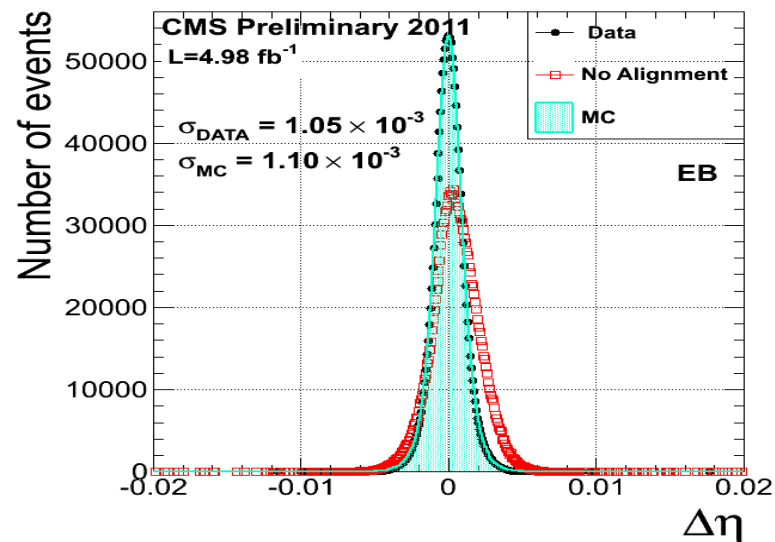
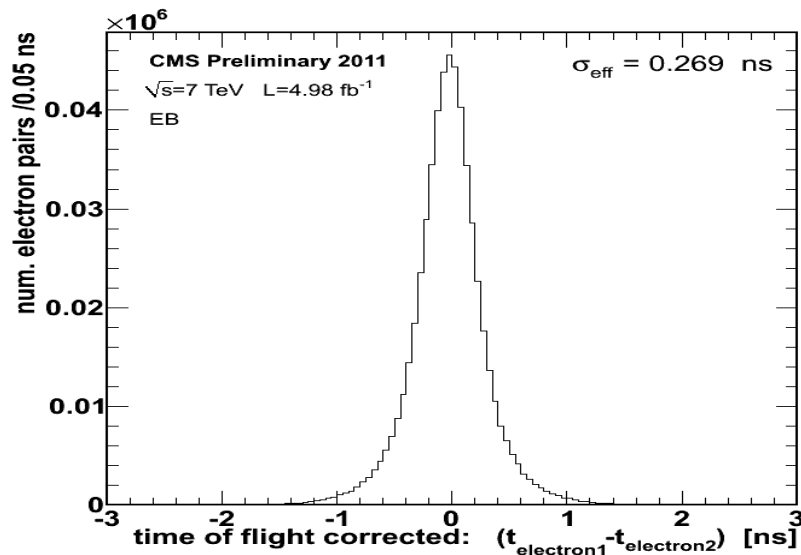


Double effort continuously ongoing to:

1. Improve the energy resolution both in Data and MC: inter-calibration precision, optimization of cluster corrections.
2. Reduce/nullify the difference between data and MC due to contributions possibly not fully simulated (improvement observed in laser correction stability, tuning of the material simulation, etc).

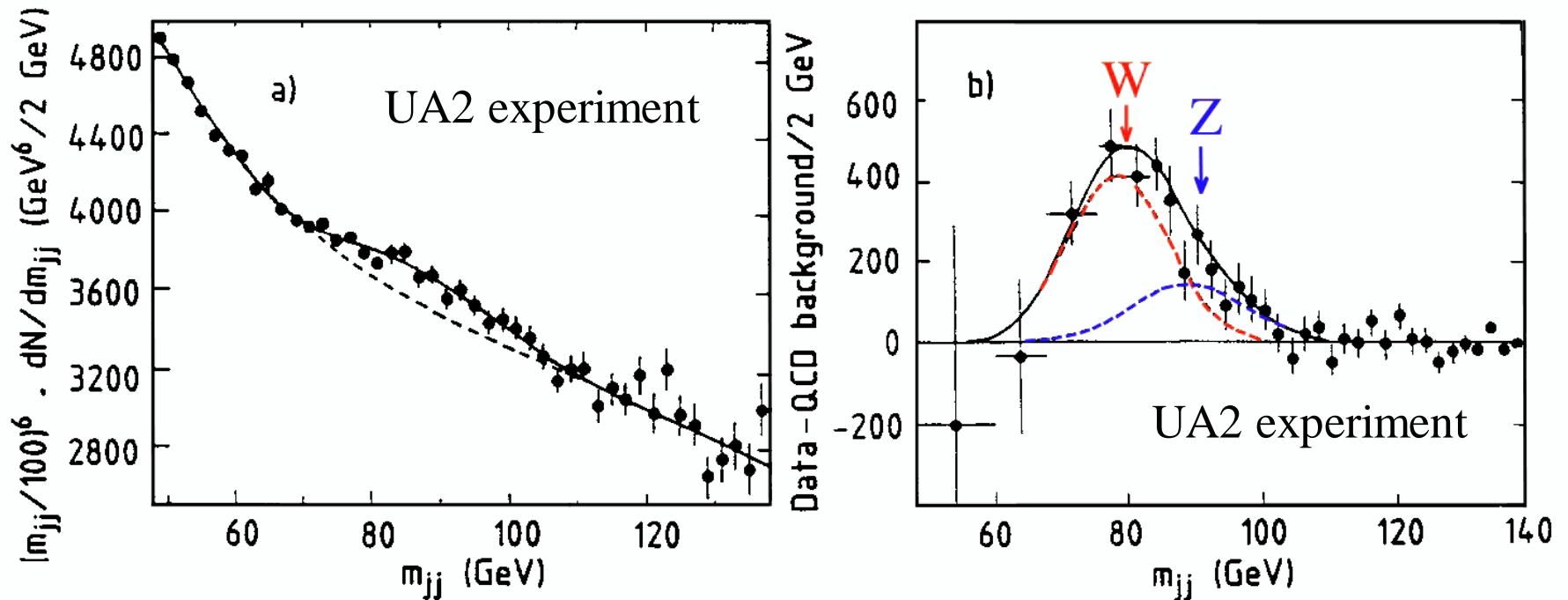
Alignment (in time and space)

- Timing fundamental in exotic long lived particle searches and in anomalous signal rejection.
- Time difference between the seed crystals for the two Z electrons.
- The time resolution for a single ECAL crystal, for the energy range of electrons from Z decays, is 0.19/0.28 ns in EB/EE.
- No longitudinal segmentation of ECAL → Photon direction from shower position and identification of the interaction vertex
- Relative alignment of the ECAL crystals and the CMS tracker measured using electrons from $Z \rightarrow ee$ and $W \rightarrow ev$ events.
- Position resolution ≤ 1 mm



Calorimeters and discoveries: a long relationship (for instance J/ Ψ , W & Z)

Final states with electrons, photons and jets also fundamental in new physics.



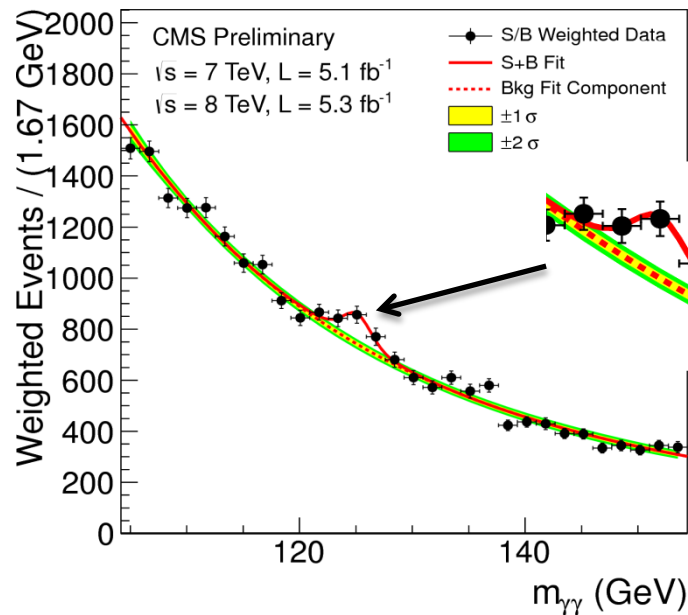
François Englert Peter W. Higgs



© The Nobel Foundation. Photo: Lovisa Engblom

Calorimeters and discoveries: a long relationship

Plot from the CMS 4th July 2012
Higgs search presentation



CMS Experiment at LHC, CERN
Data recorded: Sat May 26 08:58:34 2012 CEST
Run/Event: 195013 / 191541168
Lumi section: 466