# Particle Physics Data Analysis Tools 

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Experimental Particle Physics
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## Strategy for particle physics searches

* Find excess over SM background
* Identify models compatible with excess
* Look for predicted excesses in other channels
* Determine underlying model



## Simplified LHC event



## From theory to detector

## Lagrangian



## From theory to detector



## From theory to detector



## From theory to detector



## From theory to detector



## From theory to detector



* Mathematica package to derive Feynman rules from a Lagrangian
* Available at feynrules.irmp.ucl.ac.be

Lagrangian

FeynmanRules

Gauge symmetries


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Lagrangian
Gauge symmetries Particles Parameters Lagrangian


## FeynRules

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Lagrangian

FeynmanRules

## Gauge symmetries Particles Parameters Lagrangian

```
M$Parameters = {
    aS == {
        ParameterType
        BlockName
        OrderBlock
        Value
        InteractionOrder
        TeX
        Description
    },
    gs == {
        ParameterType
        Value
        InteractionOrder
        TeX
    ParameterName
    Description
    },[...]
```

CKM == $\{$
ParameterType $\rightarrow$ Internal,
Indices $\quad>$ \{Index[Generation], Index[Generation]\},
Unitary
$\rightarrow$ True,
$\rightarrow$ \{CKM $[1,1] \rightarrow$ Cos[cabi], CKM[1,2] $\rightarrow$ Sin[cabi],
$\rightarrow$ Cos[cabi]
CKM $[3,2] \rightarrow 0$,
CKM $[1,3] \rightarrow 0$,
CKM $[2,1]$-> -Sin[cabi]
CKM $[3,1] \rightarrow 0, \quad$ CKM $[3,2] \rightarrow 0, \quad$ CKM $[3,3] \rightarrow 1\}$,
$\operatorname{CKM}[2,3] \rightarrow 0$,
Description -> "CKM-Matrix"\}

* Mathematica package to derive Feynman rules from a Lagrangian
* Available at feynrules.irmp.ucl.ac.be
Gauge symmetries Particles Parameters Lagrangian

```
LFermions := Block[{mu},
    ExpandIndices[I*(
        QLbar.Ga[mu].DC[QL, mu] + LLbar.Ga[mu].DC[LL, mu] +
        uRbar.Ga[mu].DC[uR, mu] + dRbar.Ga[mu].DC[dR, mu] +
        lRbar.Ga[mu].DC[lR, mu]), FlavorExpand->{SU2W,SU2D}]
```

WriteUFO[LSM] $\rightarrow$
UFO becoming the standard


# MadGraph5 

[arXiv:1405.0301]

Computing amplitudes with HELAS
(HELicity Amplitude Subroutine)
Evaluate $\mathcal{M}$ for fixed helicity of external particles


FeynmanRules


$$
\mathcal{M}=\bar{u} \gamma^{\mu} v P_{\mu \nu} \bar{u} \gamma^{\nu} v
$$

# MadGraph5 

[arXiv:1405.0301]

Computing amplitudes with HELAS
(HELicity Amplitude Subroutine)
Evaluate $\mathcal{M}$ for fixed helicity of external particles

FeynmanRules


Particles

# MadGraph5 

[arXiv:1405.0301]

Computing amplitudes with HELAS (HELicity Amplitude Subroutine)
Evaluate $\mathcal{M}$ for fixed helicity of external particles

FeynmanRules


# MadGraph5 

[arXiv:1405.0301]

Computing amplitudes with HELAS
(HELicity Amplitude Subroutine)
Evaluate $\mathcal{M}$ for fixed helicity of external particles

FeynmanRules
matrix-element

$>$ Helicity amplitude routines needed for the Standard Model, MSSM, ..., in hand-written library
$>$ Any new Lorentz structure needs addition by hand $\Rightarrow$ restriction on types of models that could be implemented in MadGraph

# MadGraph5 

[arXiv:1405.0301]

Computing amplitudes with HELAS
(HELicity Amplitude Subroutine)
Evaluate $\mathcal{M}$ for fixed helicity of external particles


FeynmanRules


# MadGraph5 

[arXiv:1405.0301]

Weighting experimental events with MadWeight
$P(\boldsymbol{x}, \alpha)=$
$\begin{gathered}\text { Probability of observing } \boldsymbol{x} \\ \text { predicted by the model } \boldsymbol{\alpha}\end{gathered}$
$\boldsymbol{x}:$ experimental measurements

# MadGraph5 

[arXiv:1405.0301]


Weighting experimental events with MadWeight
$P(\boldsymbol{x}, \alpha)=$


Probability of observing $\boldsymbol{x}$ predicted by the model $\boldsymbol{\alpha}$
$x$ : experimental measurements


# MadGraph5 

[arXiv:1405.0301]

Weighting experimental events with MadWeight


# MadGraph5 

[arXiv:1405.0301]

## Weighting experimental events with MadWeight



Probability of observing $\boldsymbol{x}$ predicted by the model $\boldsymbol{\alpha}$
$x$ : experimental measurements


Resolution function
$y$ : partonic momenta (experimental extraction)

# MadGraph5 

[arXiv:1405.0301]

## Weighting experimental events with MadWeight

$$
\begin{aligned}
& P(\boldsymbol{x}, \alpha)=\frac{1}{\sigma} \int d \phi(\boldsymbol{y}) d w_{1} d w_{2} f_{1}\left(w_{1}\right) f_{2}\left(w_{2}\right)\left|M_{\alpha}\right|^{2}(\boldsymbol{y}) W(\boldsymbol{x}, \boldsymbol{y}) \\
& \begin{array}{l}
\downarrow \\
\text { Partonic phase-space measure }
\end{array} \\
& \begin{array}{l}
\downarrow \\
\text { Squared matrix element }
\end{array} \\
& \text { Paility of observing } \boldsymbol{x} \\
& \text { cted by the model } \boldsymbol{\alpha} \\
& \text { imental measurements }
\end{aligned}
$$

## MadGraph5

[arXiv:1405.0301]

Weighting experimental events with MadWeight

$$
\begin{aligned}
& \left.P(\boldsymbol{x}, \alpha)=\frac{1}{\sigma} \int \begin{array}{c}
d \phi(\boldsymbol{y}) d w_{1} d w_{2} f_{1}\left(w_{1}\right) f_{2}\left(w_{2}\right)\left|M_{\alpha}\right|^{2}(\boldsymbol{y}) W(\boldsymbol{x}, \boldsymbol{y}) \\
\downarrow \\
\text { Partonic phase-space measure }
\end{array} \begin{array}{c}
\downarrow \\
\text { Squared matrix element }
\end{array} \right\rvert\, \\
& \text { Parton Distribution }
\end{aligned}
$$

Probability of observing $\boldsymbol{x}$ predicted by the model $\boldsymbol{\alpha}$
$\boldsymbol{x}$ : experimental measurements

Functions


Resolution function
$\boldsymbol{y}$ : partonic momenta (experimental extraction)

$$
W(\boldsymbol{x}, \boldsymbol{y}) \approx \prod_{i=E, \phi, \eta} \frac{1}{\sqrt{2 \pi} \sigma_{i}} e^{-\frac{\left(x_{i}-y_{i}\right)^{2}}{2 \sigma_{i}^{2}}}
$$

$$
\text { Propagators: } \frac{1}{\left|q^{2}-M^{2}+i M \Gamma\right|^{2}}
$$

FeynmanRules

# MadGraph5 

[arXiv:1405.0301]

## Weighting experimental events with MadWeight Monte-Carlo integration



# MadGraph5 

[arXiv:1405.0301]

## Weighting experimental events with MadWeight Monte-Carlo integration




FeynmanRules

# MadGraph5 

[arXiv:1405.0301]

Weighting experimental events with MadWeight Importance sampling



## MadGraph5

[arXiv:1405.0301]

Weighting experimental events with MadWeight VEGAS (Adaptative Monte-Carlo)


FeynmanRules

Any peak is aligned along a single direction of the P-S parameterization Integration is very efficient

# MadGraph5 

[arXiv:1405.0301]

Weighting experimental events with MadWeight VEGAS (Adaptative Monte-Carlo)


Some peaks are not aligned along a single direction of the P-S parameterization Integration converges slowly

# MadGraph5 

[arXiv:1405.0301]

Weighting experimental events with MadWeight VEGAS (Adaptative Monte-Carlo)


FeynmanRules

# MadGraph5 

[arXiv:1405.0301]

Weighting experimental events with MadWeight
Multi-channel Monte-Carlo


What if there is no transformation that aligns all integrand peaks to the chosen axes?

# MadGraph5 

[arXiv:1405.0301]

Weighting experimental events with MadWeight Multi-channel Monte-Carlo



FeynmanRules

What if there is no transformation that aligns all integrand peaks to the chosen axes? Solution: use different transformations (channels)

$$
p(x)=\sum_{i=1}^{n} \alpha_{i} p_{i}(x) \quad \sum_{i=1}^{n} \alpha_{i}=1
$$

# MadGraph5 

[arXiv:1405.0301]

Weighting experimental events with MadWeight
Example


FeynmanRules


Three very different pole structures contributing to the same matrix element

$$
\begin{gathered}
p(x)=\sum_{i=1}^{n} \alpha_{i} p_{i}(x) \quad \sum_{i=1}^{n} \alpha_{i}=1 \\
\int\left|M_{t o t}\right|^{2}=\int \frac{\sum_{i}\left|M_{i}\right|^{2}}{\sum_{j}\left|M_{j}\right|^{2}}\left|M_{t o t}\right|^{2}=\sum_{i} \int \frac{\left|M_{i}\right|^{2}}{\sum_{j}\left|M_{j}\right|^{2}}\left|M_{t o t}\right|^{2}
\end{gathered}
$$

# MadGraph5 

[arXiv:1405.0301]

Generating events with MadEvent



# MadGraph5 

[arXiv:1405.0301]

Generating events with MadEvent



# MadGraph5 

[arXiv:1405.0301]

Generating events with MadEvent



# MadGraph5 

[arXiv:1405.0301]

Generating events with MadEvent



FeynmanRules
matrix-element
parton events

# MadGraph5 

[arXiv:1405.0301]

Generating events with MadEvent



Same number of events in areas of phase space with different probabilities
Events must have different weights (weighted)

# MadGraph5 

[arXiv:1405.0301]

Generating events with MadEvent



FeynmanRules

parton events

Number of events is proportional to the probability of areas of phase space Events have the same weight (unweighted)

Events distributed as in nature


Matching to parton shower



Matching to parton shower



FeynmanRules
matrix-element
! ! !


Matching to parton shower



FeynmanRules
! ! !
matrix-element

## r



Matching to parton shower


Matching to parton shower


## Detector simulation tools



## Detector simulation tools



Fast detector simulation for phenomenological studies
Based on the parameterization of the detector response


FeynmanRules
$\frac{?}{\text { matrix-element }}$
matrix-element

hower/hadronize events

Detector events

## Delphes

Fast detector simulation for phenomenological studies Based on the parameterization of the detector response




No real tracking in Delphes

## GEANT

[0.1109/TNS.2006.869826]

GEometry ANd Tracking
A Monte Carlo software toolkit to simulate the passage of particles through matter


Lagrangian

FeynmanRules


Detector events


## Particle-Matter interaction

## Digitization



## GEANT

[0.1109/TNS.2006.869826]

## G Geant4

## Particle-Matter interaction

$>$ Describe the geometry and the material of the detector


## GEANT

[0.1109/TNS.2006.869826]

## Particle-Matter interaction

$>$ Describe the geometry and the material of the detector
$>$ Treat a particle at a time

## GEANT

[0.1109/TNS.2006.869826]

## G) Geant4

## Particle-Matter interaction

$>$ Describe the geometry and the material of the detector
> Treat a particle at a time
$>$ Trajectory of the particle is split in steps (finite displacements)
a point where a physics
process occurred
start point


## GEANT

## [0.1109/TNS.2006.869826]

## Particle-Matter interaction

> Describe the geometry and the material of the detector
> Treat a particle at a time
$>$ Trajectory of the particle is split in steps (finite displacements)
$>$ Simulate the physics along a step and at the end of each step


Elastic scattering


Inelastic scattering


Bremsstrahlung emission

## GEANT

[0.1109/TNS.2006.869826]

## Particle-Matter interaction

$>$ Describe the geometry and the material of the detector
> Treat a particle at a time
$>$ Trajectory of the particle is split in steps (finite displacements)
$>$ Simulate the physics along a step and at the end of each step

$>$ convert the energy deposit into electric signal

## GEANT

[0.1109/TNS.2006.869826]

## Particle-Matter interaction



## Digitization

$>$ convert the energy deposit into electric signal
> Identify the sensitive part of the detector

## GEANT

[0.1109/TNS.2006.869826]

## Particle-Matter interaction



## Digitization

$>$ convert the energy deposit into electric signal
$>$ Identify the sensitive part of the detector

- Modelize detector answer


## GEANT

## MC Simulation of Particle Interactions with Matter


$>$ The exponential law:
$P(x)$ : probability of not having an interaction after a distance $x$ $w d x: p r o b a b i l i t y ~ o f ~ h a v i n g ~ a n ~ i n t e r a c t i o n ~ b e t w e e n ~ x a n d ~ x+d x$
depends on
material and
physical process

$$
P(x+d x)=P(x)(1-w d x)
$$

$$
P(x)=e^{-w x} \quad P_{\text {int }}(x)=1-e^{-w x}
$$

matrix-element


Now use the inverse method to generate an interaction:

$$
P_{\text {int }}=\alpha: \text { uniform random number of }[0,1] \Rightarrow x w=-\ln (1-\alpha)
$$

Particle Transportation: How to Determine a Step


## Particle Transportation: How to Determine a Step

1) Evaluate $\boldsymbol{x}$ using $\alpha, w$ for each physical process independently $(x w=-\ln (1-\alpha))$


## GEANT

[0.1109/TNS.2006.869826]

## 9 Geant4 <br> A simuLation toolkit

## Particle Transportation: How to Determine a Step

1) Evaluate $x$ using $\alpha, w$ for each physical process independently $(x w=-\ln (1-\alpha))$
2) Compare: process with minimum $\boldsymbol{x}$ determines the step length


## GEANT

[0.1109/TNS.2006.869826]

## G Geant4

## Particle Transportation: How to Determine a Step

1) Evaluate $x$ using $\alpha, w$ for each physical process independently $(x w=-\ln (1-\alpha))$
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3) Transport particle for the determined step


## GEANT

## Particle Transportation: How to Determine a Step

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4) If the particle is still alive after the interaction, do the sampling again and continue transportation


## GEANT

## Particle Transportation: How to Determine a Step

1) Evaluate $x$ using $\alpha, w$ for each physical process independently $(x w=-\ln (1-\alpha))$
2) Compare: process with minimum $\boldsymbol{x}$ determines the step length
3) Transport particle for the determined step
4) If the particle is still alive after the interaction, do the sampling again and continue transportation
5) If the particle disappears after the interaction, then the transportation is
 terminated


## GEANT

## [0.1109/TNS.2006.869826]

## G Geant4 <br> A simulation tookit










## ROOT

[10.1016/S0168-9002(97)00048-X]

ROOT is written in C++ and is designed for

- Data processing
- Data analysis
- Data visualization
- Data storage

Widely used in High Energy Physics and other sciences/industry

- Can be used for petabytes/year rates of data

FeynmanRules


* Provides Python Bindings C++


## ROOT

[10.1016/S0168-9002(97)00048-X]

* Modes of work:
- Interactive (ROOT prompt with CLING interpreter)
- interpretted C++ commands
- Macros : interpretted or (Just In Time) compiled
- As compilable C++ code : using Root libraries

Lagrangian

FeynmanRules


## 8

parton events

hower/hadronize events
https://root.cern
(c) 1995-2020, The ROOT Team; conception: R. Brun, F. Rademakers Built for linuxx8664gcc on Nov 27 2020, 15:14:08
From tags/v6-22-06@v6-22-06
ROOT
Try '.help', '.demo', '.license', '.credits', '.quit'/'.q'
root [0]

* Examples of what ROOT provides:

* Examples of what ROOT provides:
> Histograms, graphs, trees, ntuples: TH1,TGraph,TTree,TNtuple


## Histograms




Lagrangian

FeynmanRules
matrix-element
?
parton events


ROOT

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## Graphs




FeynmanRules


ROOT

* Examples of what ROOT provides:
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## Trees

- Data structure provided to store large quantities of objects
- Organized in branches, each one holding objects
- Organized in independent events, e.g. collision events
- Efficient disk space usage, optimized I/O runtime

* Examples of what ROOT provides:
$>$ Histograms, graphs, trees, ntuples: TH1,TGraph,TTree,TNtuple


## Ntuples

A simplified version of the TTree: store only floating point numbers



ROOT
[10.1016/S0168-9002(97)00048-X]

* Examples of what ROOT provides:
> Histograms, graphs, trees, ntuples: TH1,TGraph,TTree,TNtuple
$>$ Statistical tools: RooFit/RooStats


FeynmanRules


ROOT

## ROOT

[10.1016/S0168-9002(97)00048-X]

* Examples of what ROOT provides:
> Histograms, graphs, trees, ntuples: TH1,TGraph,TTree,TNtuple
> Statistical tools: RooFit/RooStats
$>$ A rich collection of functions (also user-defined functions: TF1)
$[0]^{*} \sin \left([1]^{*} x\right) / x$


[10.1016/S0168-9002(97)00048-X]

$>$ Histograms, graphs, trees, ntuples: TH1,TGraph,TTree,TNtuple
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> Multivariate Analysis: TMVA (e.g. Boosted decision trees, neural networks)



FeynmanRules
matrix-element
昌
parton events


ROOT

## ROOT

[10.1016/S0168-9002(97)00048-X]


FeynmanRules
matrix-element
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parton events
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hower/hadronize events


## ROOT

[10.1016/S0168-9002(97)00048-X]

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> Multivariate Analysis: TMVA (e.g. Boosted decision trees, neural networks)
$>$ Geometry Toolkit: represent geometries as complex as detectors
> Event Display (EVE): visualize particles collisions in detectors

[10.1016/S0168-9002(97)00048-X]



## ROOT

［10．1016／S0168－9002（97）00048－X］
＊Examples of what ROOT provides：
＞Histograms，graphs，trees，ntuples：TH1，TGraph，TTree，TNtuple
＞Statistical tools：RooFit／RooStats
$>$ A rich collection of functions（also user－defined functions：TF1）
$>$ Multivariate Analysis：TMVA（e．g．Boosted decision trees，neural networks）
$>$ Geometry Toolkit：represent geometries as complex as detectors
＞Event Display（EVE）：visualize particles collisions in detectors
＞PyROOT：bindings to interface to Python

## Lagrangian



Reyman
＞PROOF：parallel analysis facility
－Run in parallel on a large number of computers
－Proof－lite：use multiple cores to run on a desktop machine

## We will see how to use the packages in the hands on session



